

# **Space-Based Imaging Astrometry: Life with an Undersampled PSF**

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# Overview of the Talk

- **Astrometry with HST**
  - 3 critical issues
  - Science
    - General
    - Microlensing
- **Extensions to WFIRST**

# Astrometry with HST

- **One of the original selling points**
  - FGS: always planned
  - Also intended imaging astrometry
- **Several challenges**
  - 1) Undersampling → PSFs
  - 2) Distortion (several sources)
  - 3) Differential astrometry → Transformations

.... took several years to address these issues.

**Goal of talk: an appreciation of the issues  
and possibilities**

# Astrometry:

## Fundamental limitations

- **Poisson statistics**

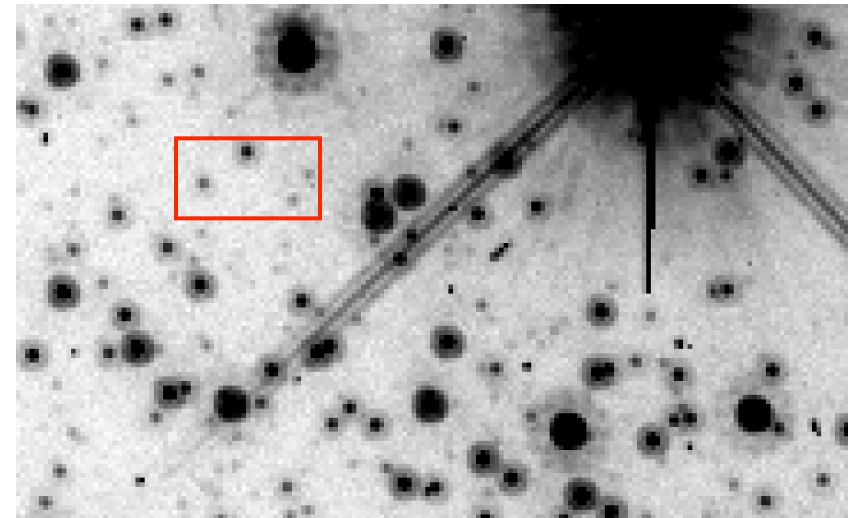
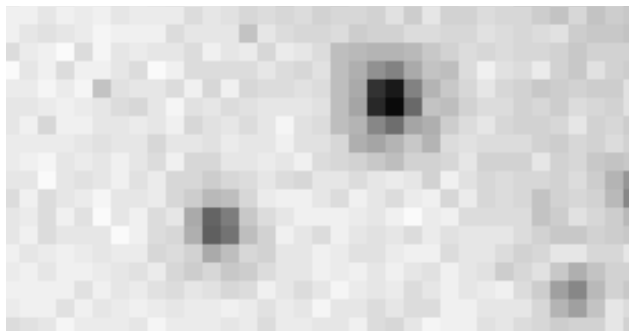
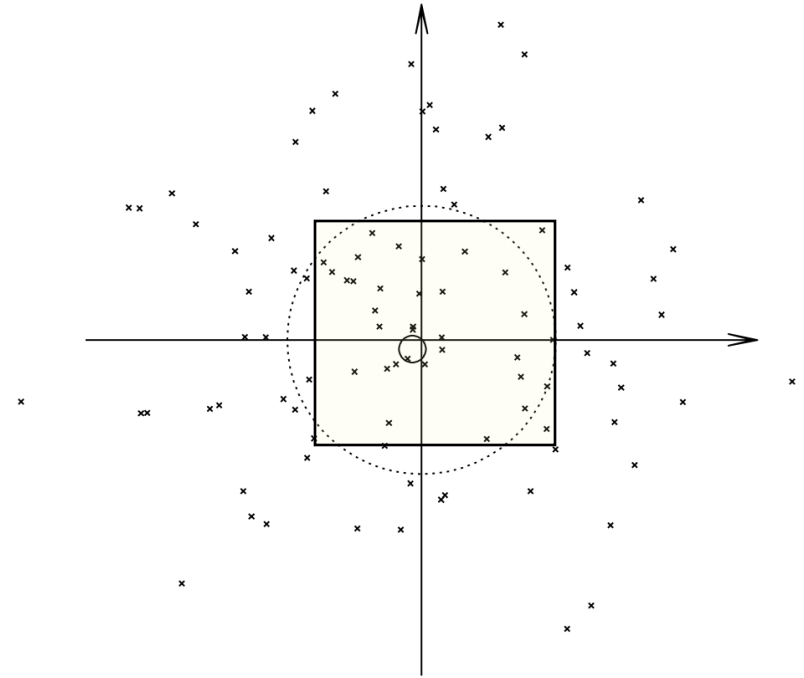
- Gaussian PSF

$$\delta x \sim \sigma_x / \sqrt{N}$$

- Best position: straight centroid

- **Pixelization**

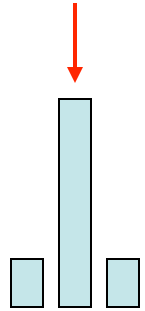
- Complication: loses information
- Simple centroid no longer works
- Requires good PSF



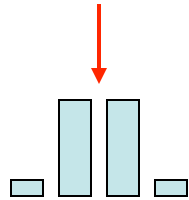
**WFC3/UVIS SWEEPS FIELD**

# Illustration of Undersampling

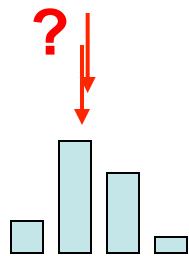
Where is the center?



Easy



Easy



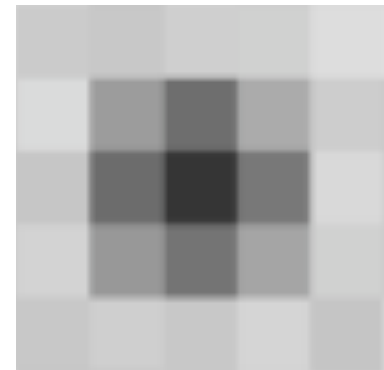
Harder

**We need an accurate PSF!**



# Undersampling and Astrometry

- **Impossible?**
  - A point source has “no hair”
  - Overconstrained problem
    - 3 parameters (x,y,f), ~9 pixels
  - Minimal requirements: “slosh”
    - Only pathological if  $\text{FWHM} < 1$  pixel
- **What is possible?**
  - 0.005-0.01 pixel possible  $\sim (S/N)^{-1}$
  - Need good PSF model
  - Need good dithering
- **Limitations**
  - Individual images; do **not** use stacks
  - Harder in crowded/sparse fields
  - Ideal in “semi-crowded” regime



# PSFs: Photometry -vs- Astrometry

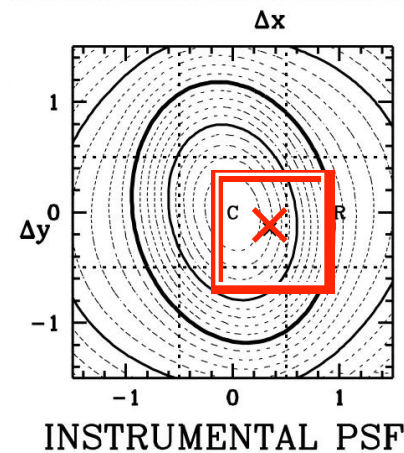
- **Photometry: how much flux is there? (SUMS)**
- **Astrometry: where is the flux? (DIFFERENCES)**
- **Shape: *exactly* where is flux... (DIFFs of DIFFs)**
  - All require good PSF, but they make different demands
- **PSF Modeling**
  - Ground
    - Variable-seeing dominated
    - Gaussian-fitting models, DAOPhot
  - HST
    - Stable but undersampled, new regime
    - Exquisitely precise models possible

# What do we mean by the PSF?

- $\psi_{\text{INST}}(\Delta\mathbf{x},\Delta\mathbf{y})$ : the “Instrumental” PSF:
  - The PSF as it hits the detector
  - Good theoretical motivations: Gaussians, Moffat
  - See  $\psi_{\text{INST}}$  only *indirectly* in images
    - Must deconvolve the PSF from the pixels
    - Saving grace: often solve for limited set of parameters
- $\psi_{\text{EFF}}(\Delta\mathbf{x},\Delta\mathbf{y})$ : the “Effective” PSF:
  - The PSF after pixelization:  $\psi_{\text{EFF}} = \psi_{\text{INST}} \otimes \Pi$
  - Empirical: no natural basis function to describe
  - Tod Lauer’s 1999 tutorial in PASP on image reconstruction
    - **OLD**: Pixels as light buckets
    - **NEW**: Pixels as point-samplings of a continuous scene
  - **Epiphany**: we *never* deal with anything BUT the effective PSF
    - See  $\psi_{\text{EFF}}$  *directly* in images
    - Can measure  $\psi_{\text{EFF}}$  directly from images



# The “Effective” PSF



- **What it represents:**

- Fraction of light that falls in a pixel, relative to the center of the star

- **Modeling images:**

OLD:  $P_{ij} = S + F_* \times \iint_{x,y \in (i,j)} \psi_{\text{INST}}(x-x_*, y-y_*) dx dy$

NEW:  $P_{ij} = S + F_* \times \psi_{\text{EFF}}(i-x_*, j-y_*)$

- **How to “see” it:**

$$\psi_{\text{EFF}}(\Delta x, \Delta y) = (P_{ij} - S) / F_*$$

- Where:  $\Delta x = i - x_*$ , etc
- We have to know  $(x_*, y_*)$  and  $F_*$

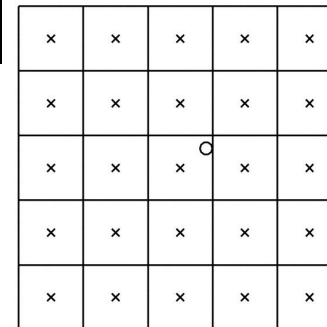
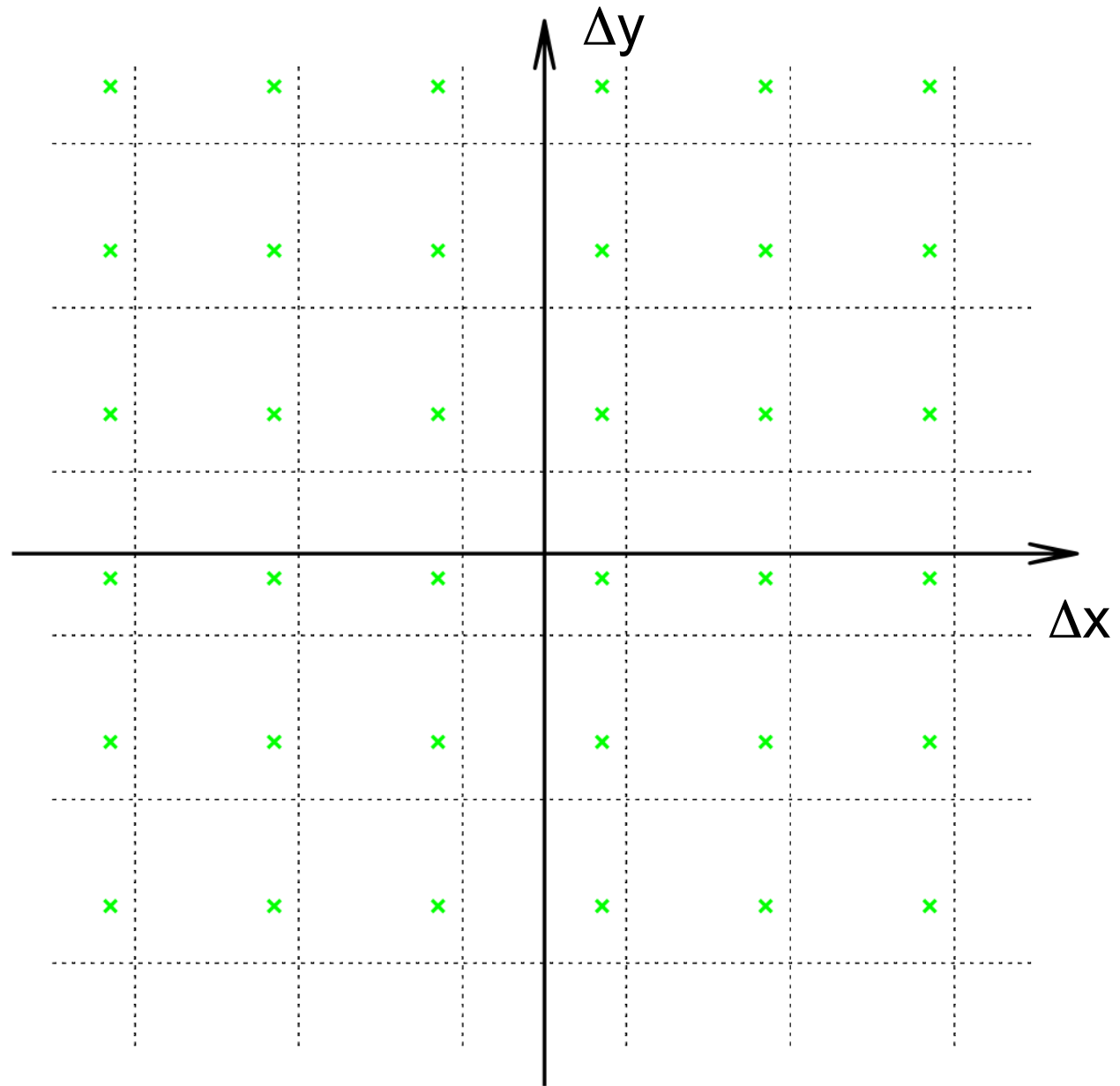


IMAGE FRAME

# How a single star samples

$$\psi_E(\Delta x, \Delta y)$$

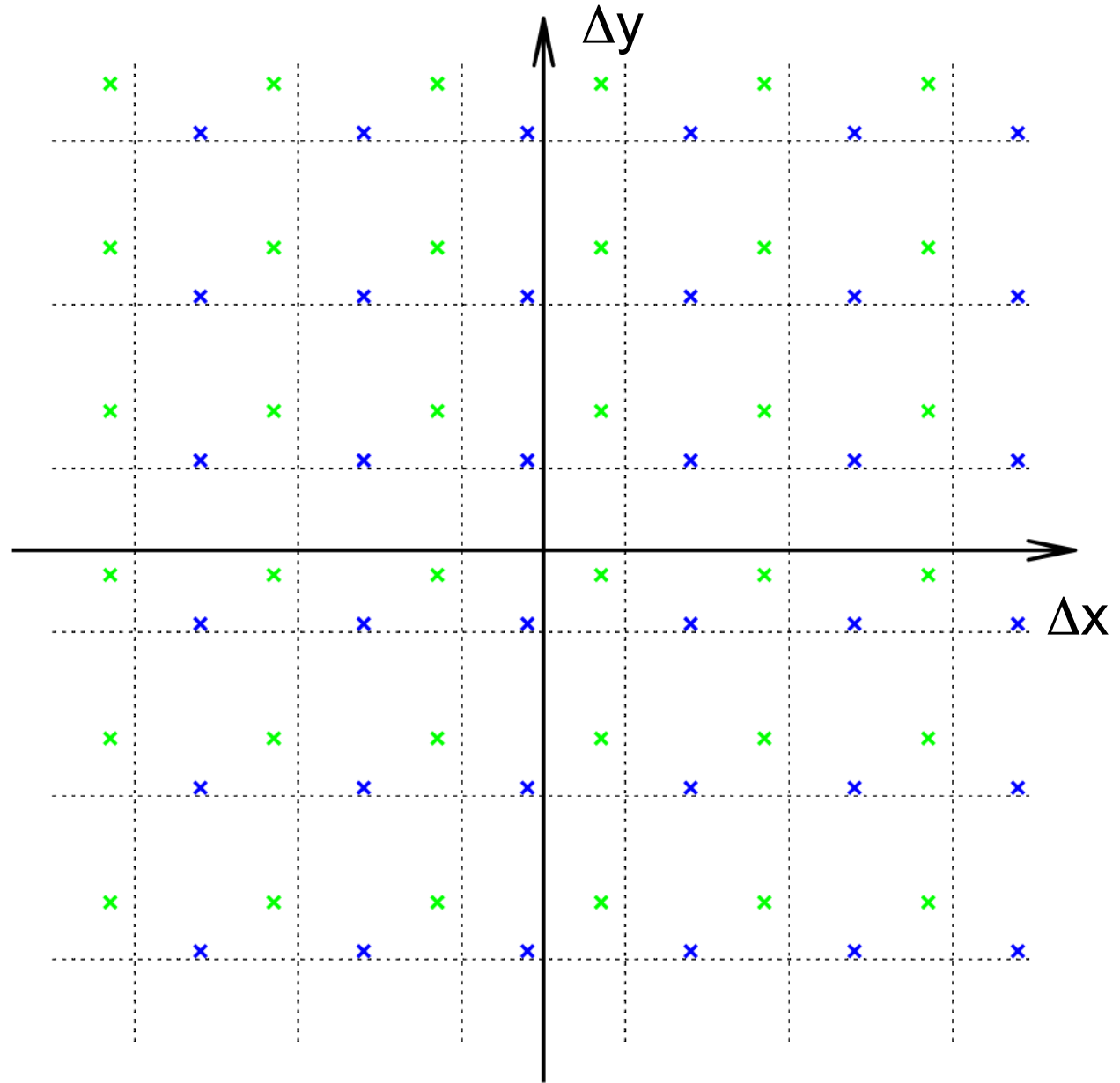
- A single star has an array of pixels about its center.
- Each pixel contains a fraction of its flux.
- Each pixel reports  $\psi_E$  at one point in  $\psi_E$ 's domain.



# How two stars

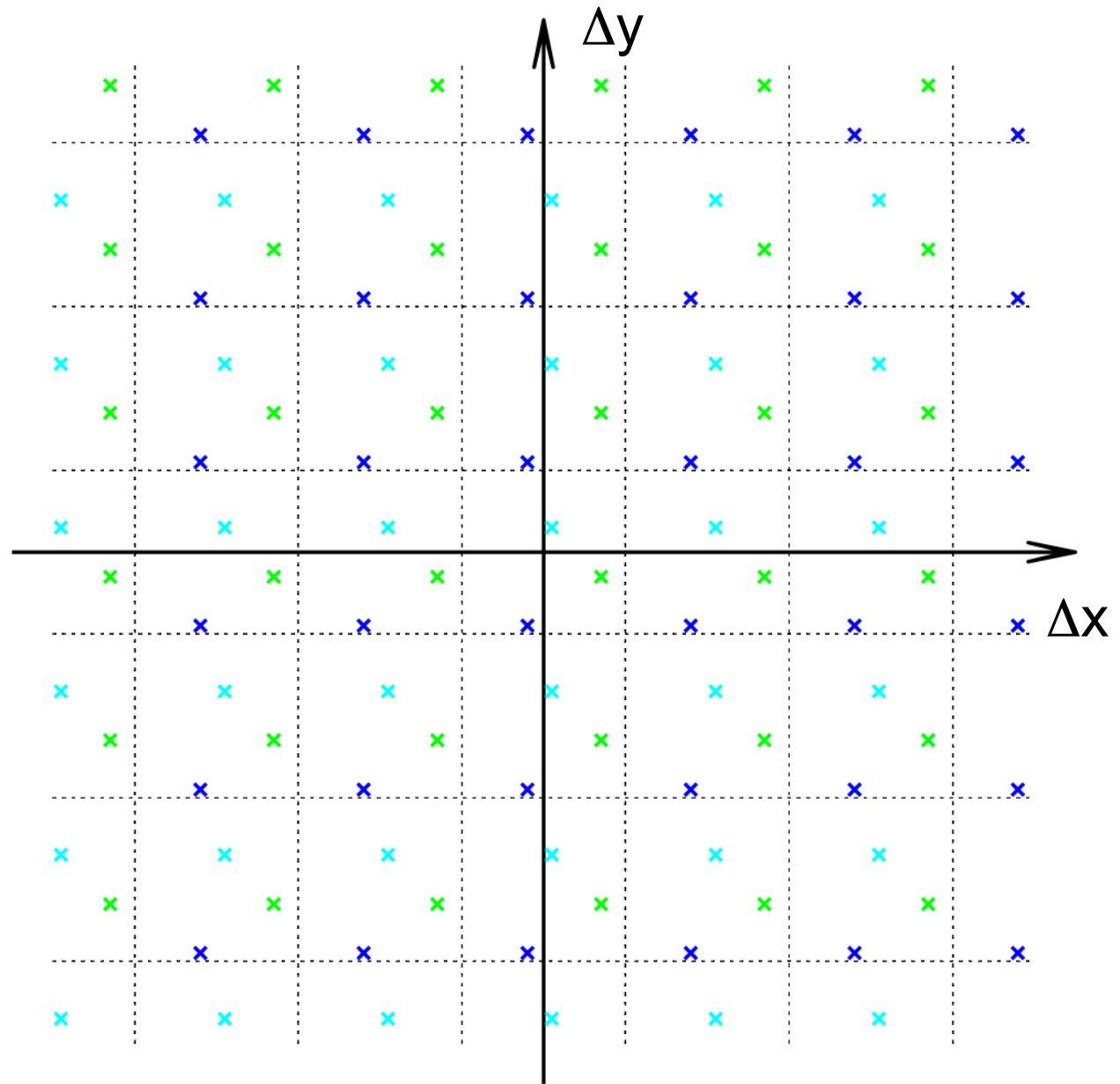
$\psi_E(\Delta x, \Delta y)$

- In general, the two stars will be at different pixel phases.
- This gives us a different array of samples of  $\psi_E$



# How three stars sample $\psi_E(\Delta x, \Delta y)$

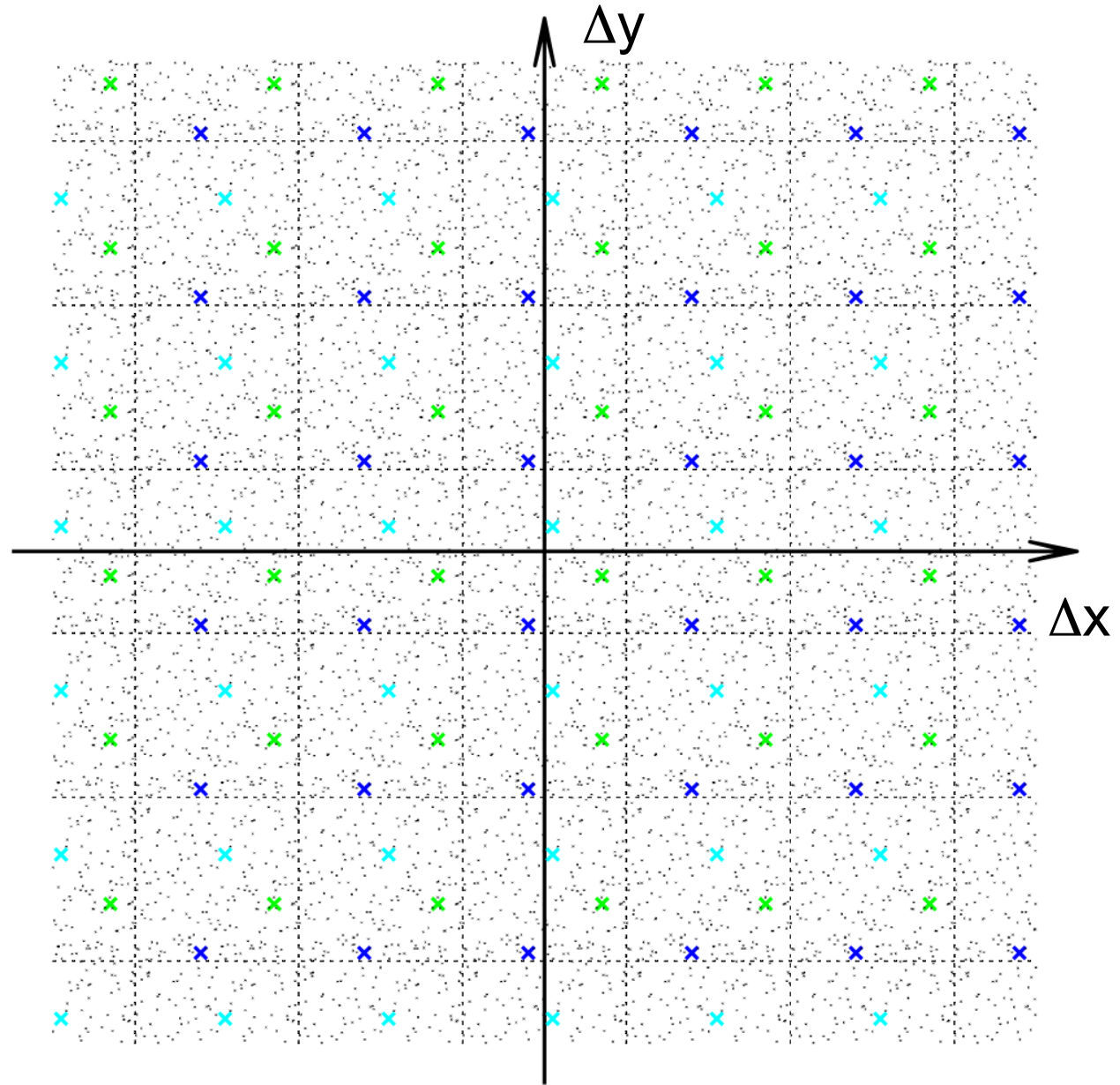
- A third star will give yet more variety in our sampling of  $\psi_E$



# How 200 stars sample

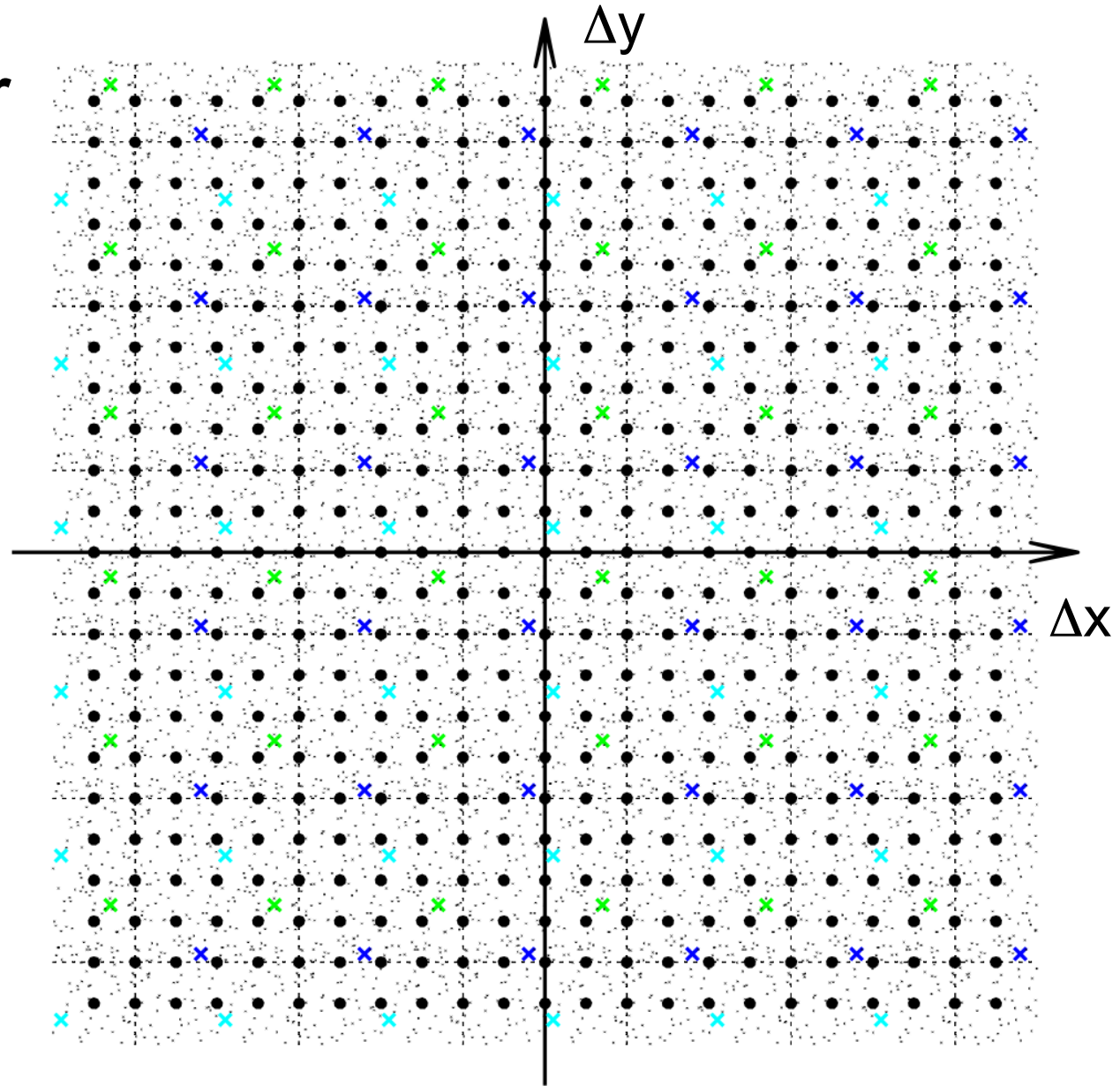
$$\psi_E(\Delta \mathbf{s}, \Delta \mathbf{y})$$

- A large number of stars gives us an almost even coverage of  $\psi_E$  across its 2-D domain.

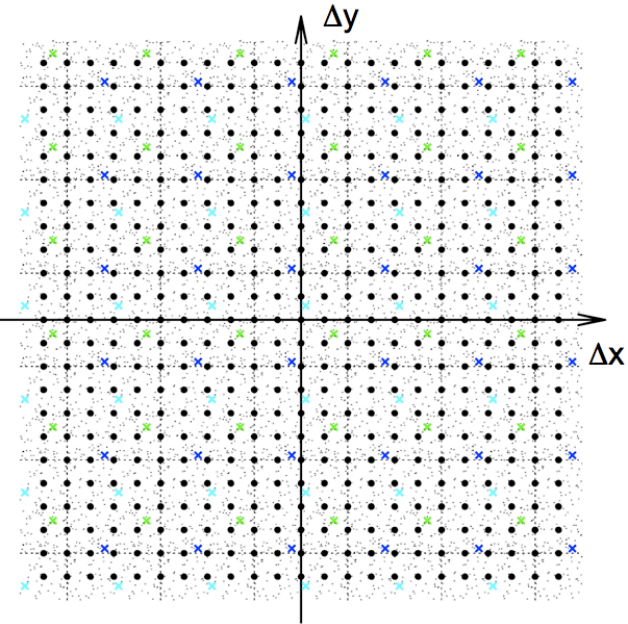


# How to solve for $\psi_E(\Delta x, \Delta y)$

- A regularly-spaced array of grid-points
- Specify value of  $\psi_E$  at those points to best-fit the data.



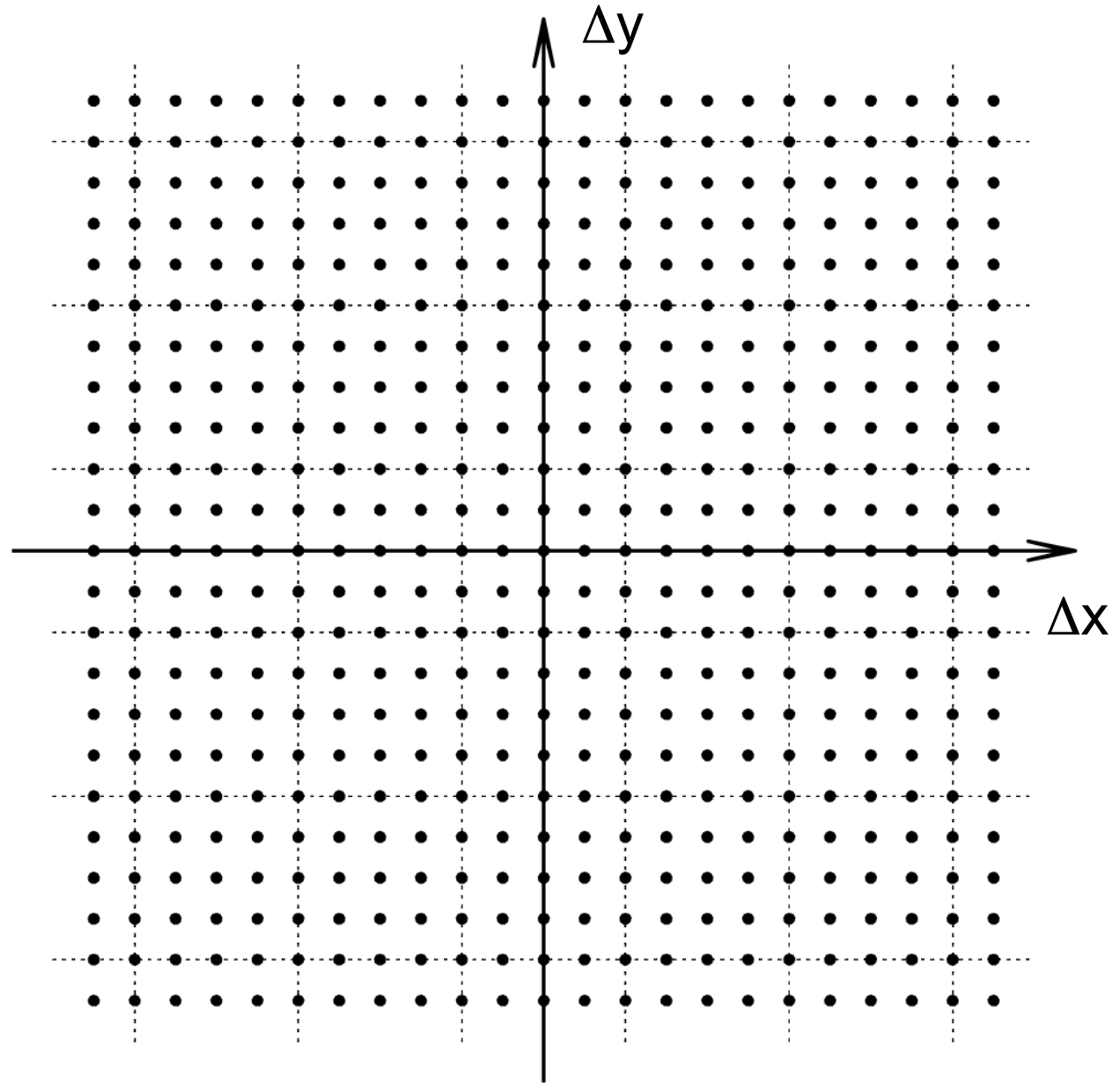
# “Seeing” $\psi_{\text{EFF}}$ Directly



# The model of

$$\psi_E(\Delta x, \Delta y)$$

- Tabulated values of  $\psi_E$  at this array of points across its domain.





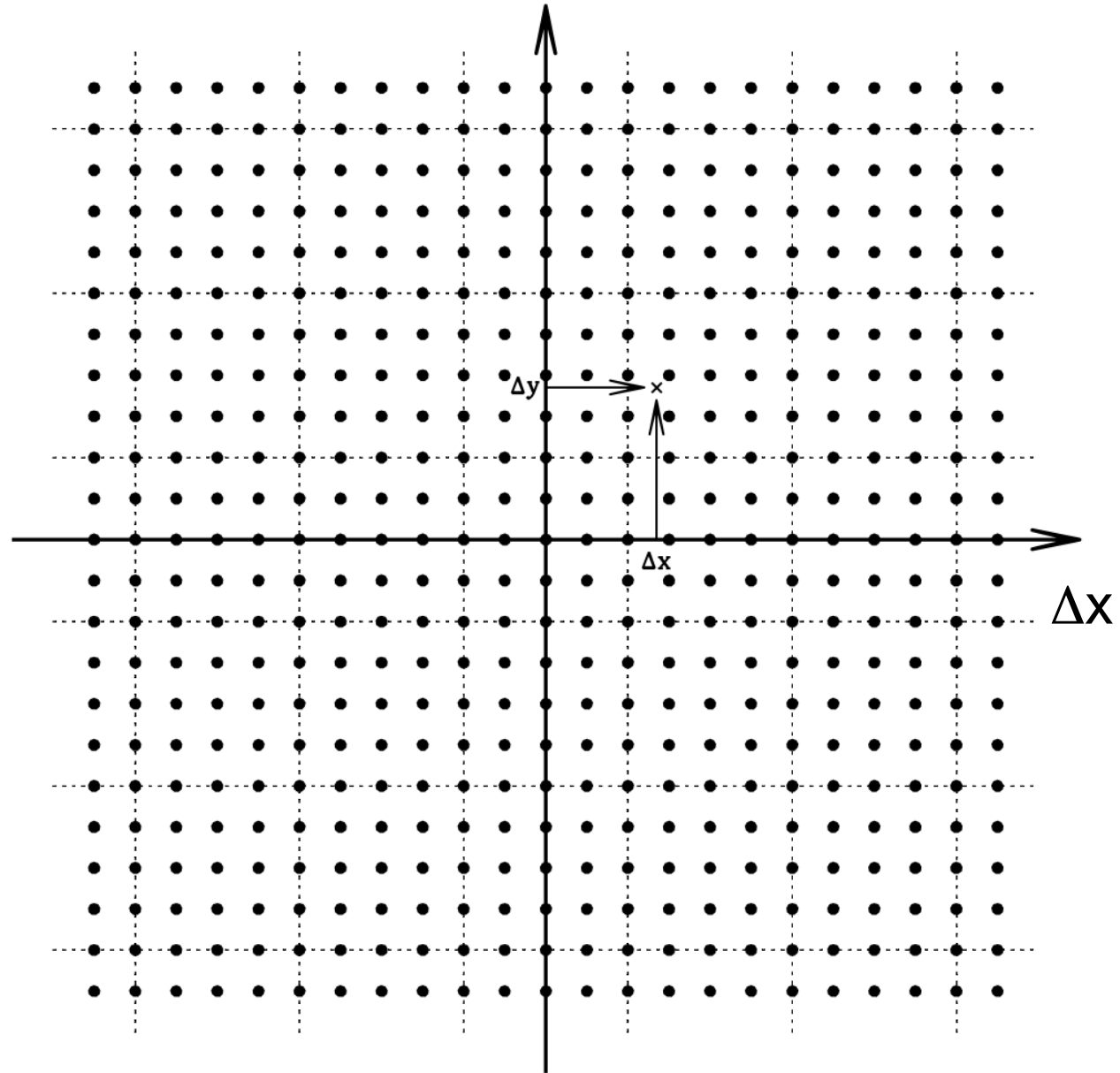
# How to use $\psi_E(\Delta x, \Delta y)$

## Need to know:

“What fraction of light should land in a pixel, if the pixel is centered at  $(\Delta x, \Delta y)$  relative to the point source?”

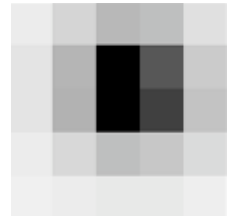
## Need to interpolate:

→ Use bi-cubic interpolation



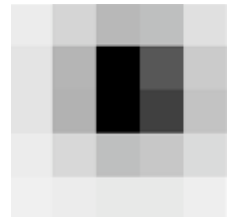
1) How to find the PSF?

**2) How to use the PSF?**



# 1) How to find the PSF?

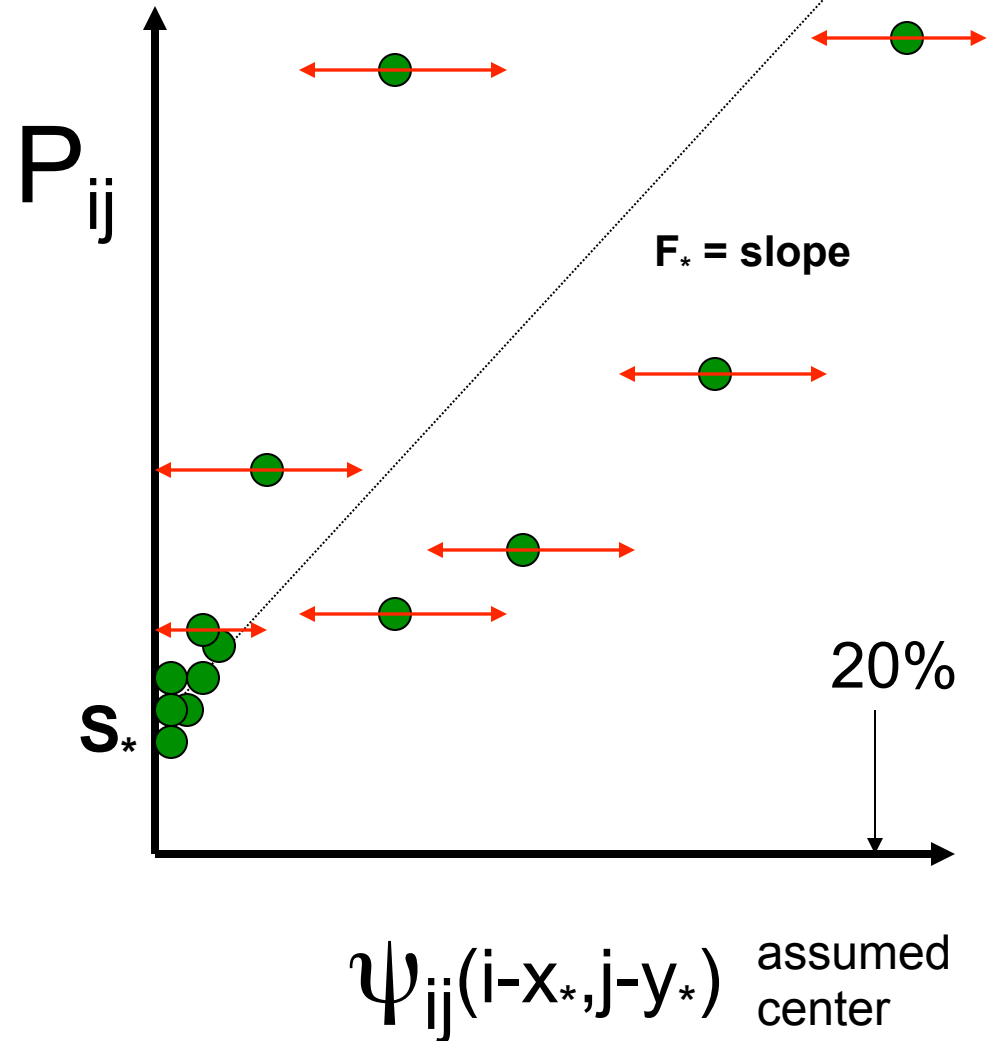
# 2) How to use the PSF?



Fitting for Flux and position:

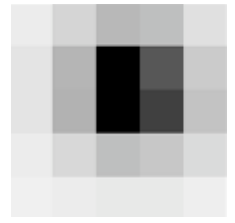
$$P_{ij} = S + F_* \times \psi_{ij}$$

- Nice, linear equation!
- Which pixels to use?



# 1) How to find the PSF?

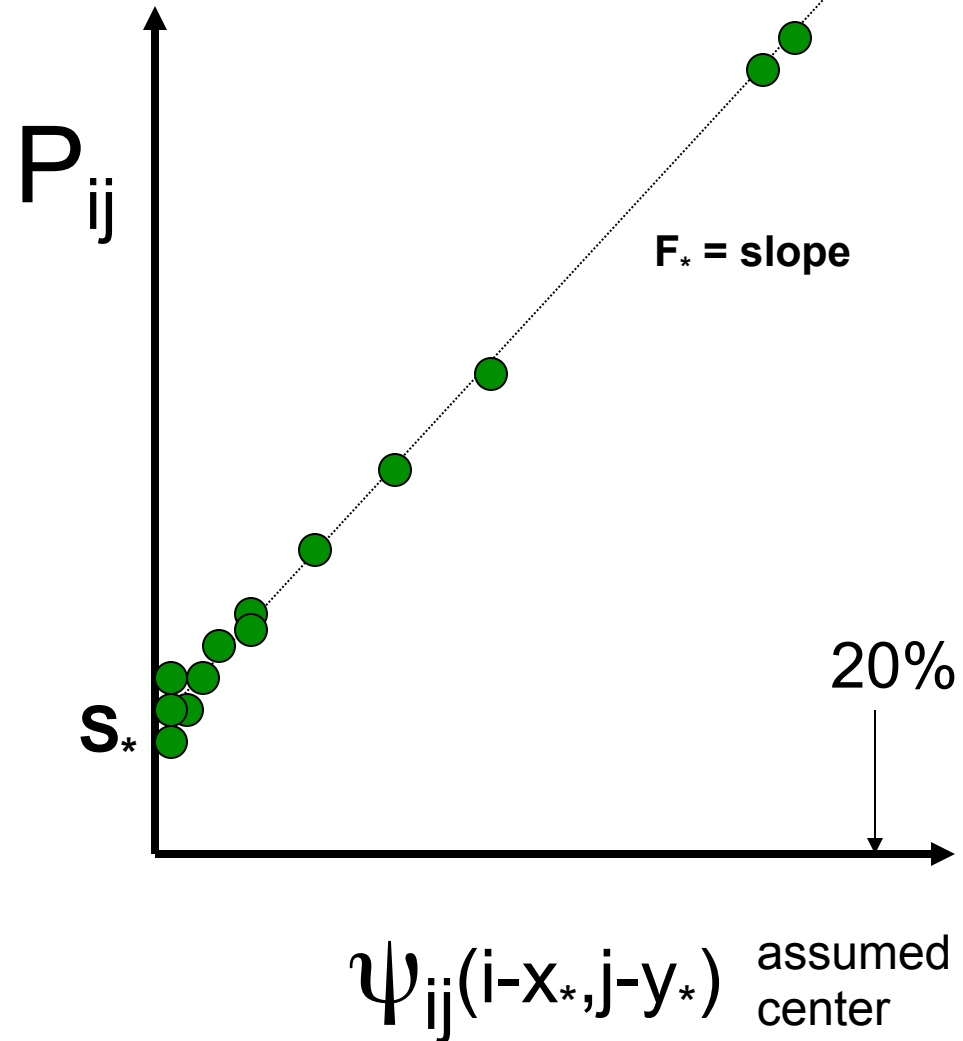
## 2) How to use the PSF?



Fitting for Flux and position:

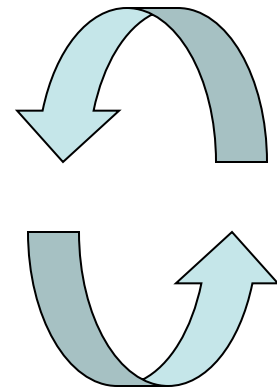
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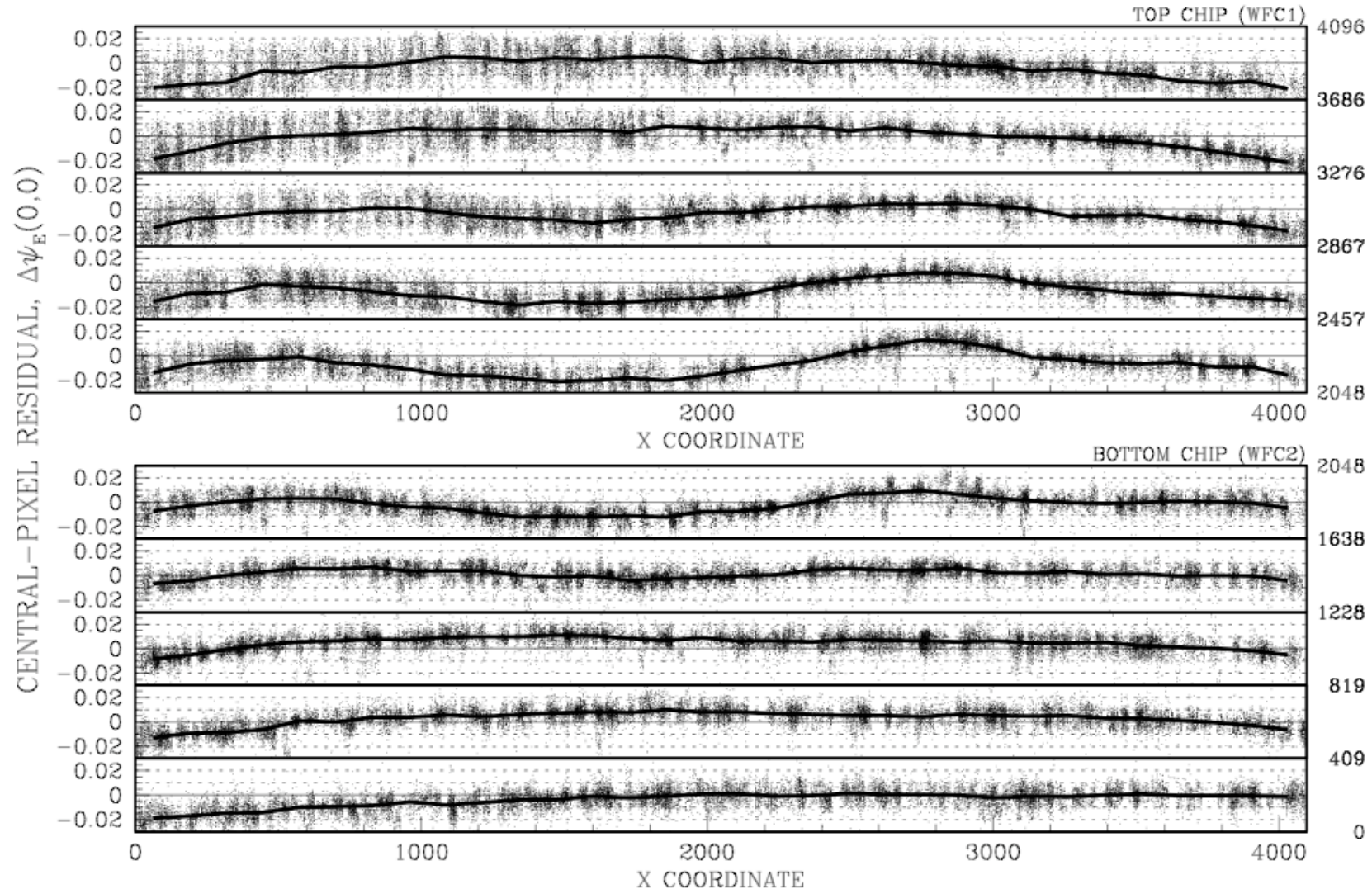
# PSF: Finding -vs- Using

- **Degeneracy:**
  - Finding  $\psi_{\text{EFF}}$  requires  $(x,y,f)$
  - Finding  $(x,y,f)$  requires  $\psi_{\text{EFF}}$
- **Iteration**
  - Dithers break the degeneracy!



# Higher-Level PSF Issues...

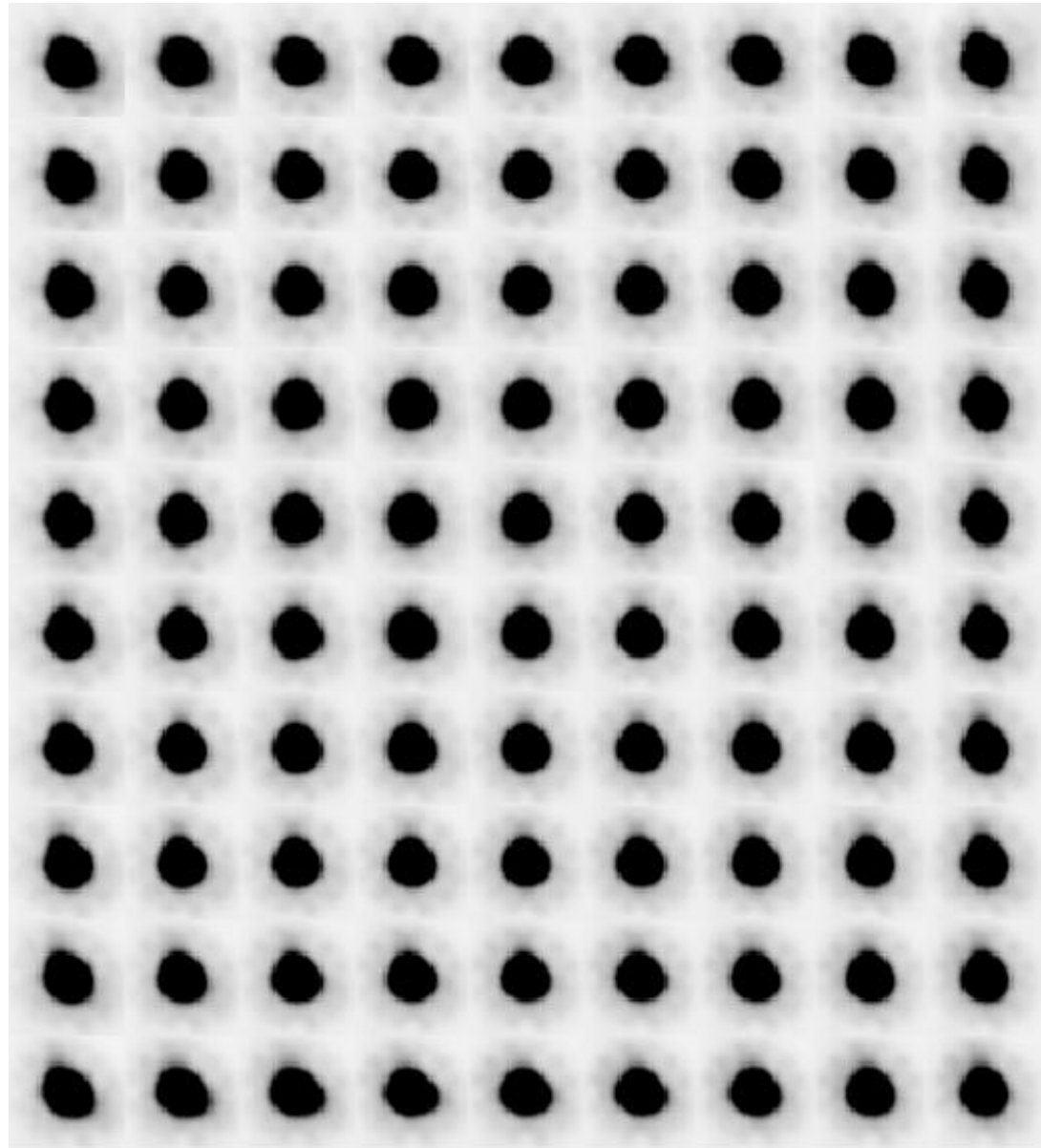
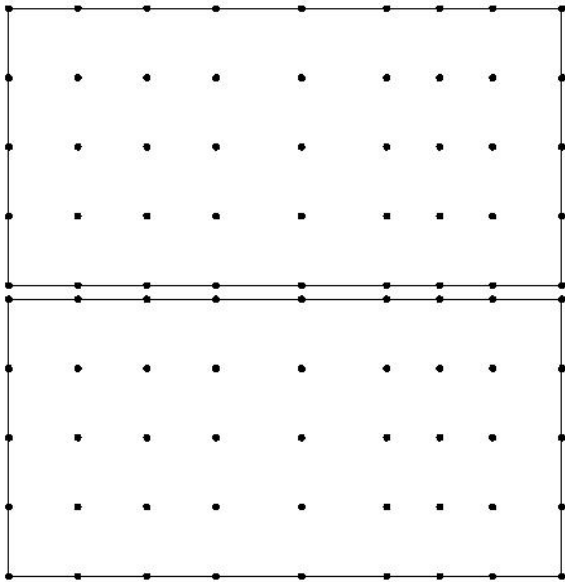
- Spatial variability...



# Higher-Level PSF Issues...

- Spatial variability...

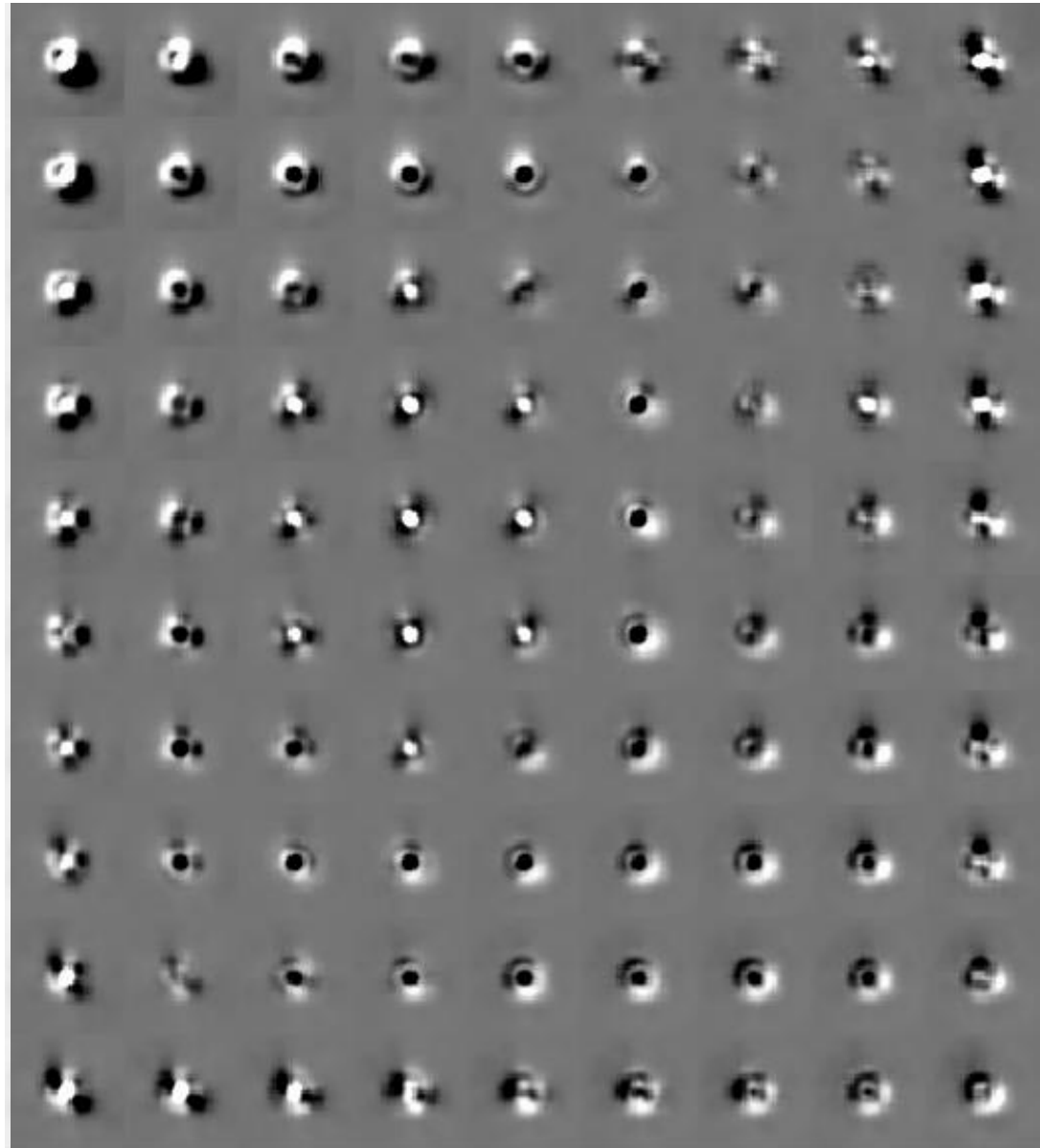
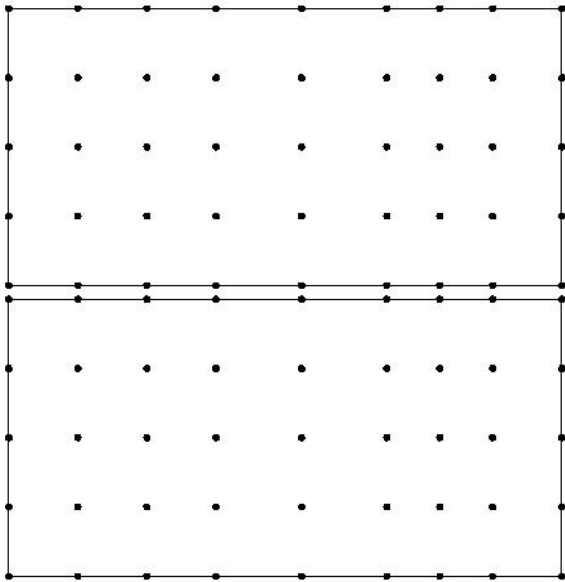
Array of PSFs for  
F606W ACS



# Higher-Level PSF Issues...

- Spatial variability...

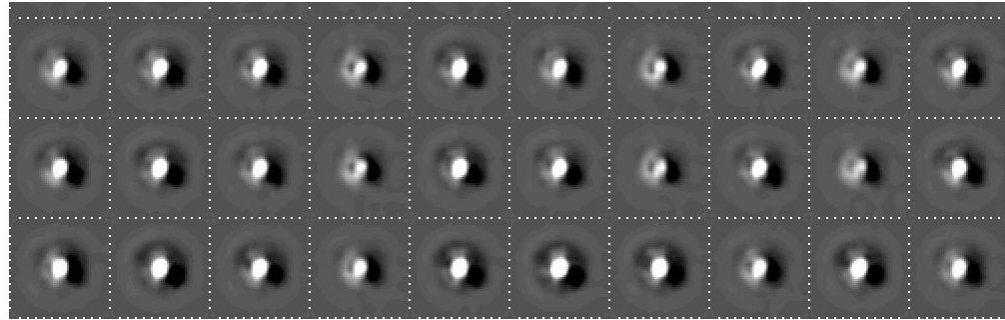
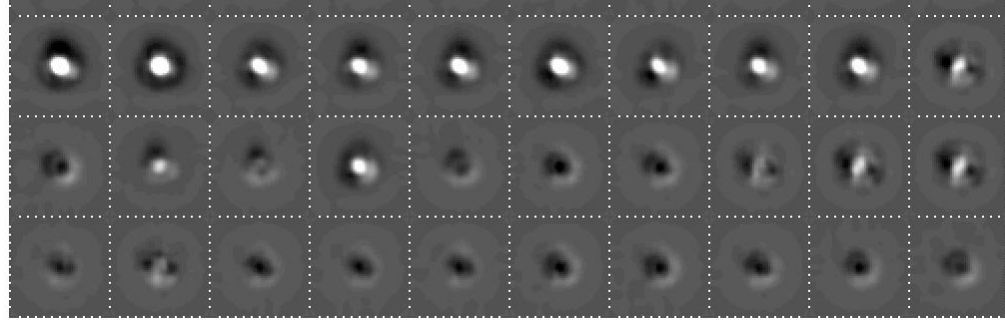
Core intensity varies  
by  $\pm 10\%$  over scales  
of  $\sim 500$  pixels.





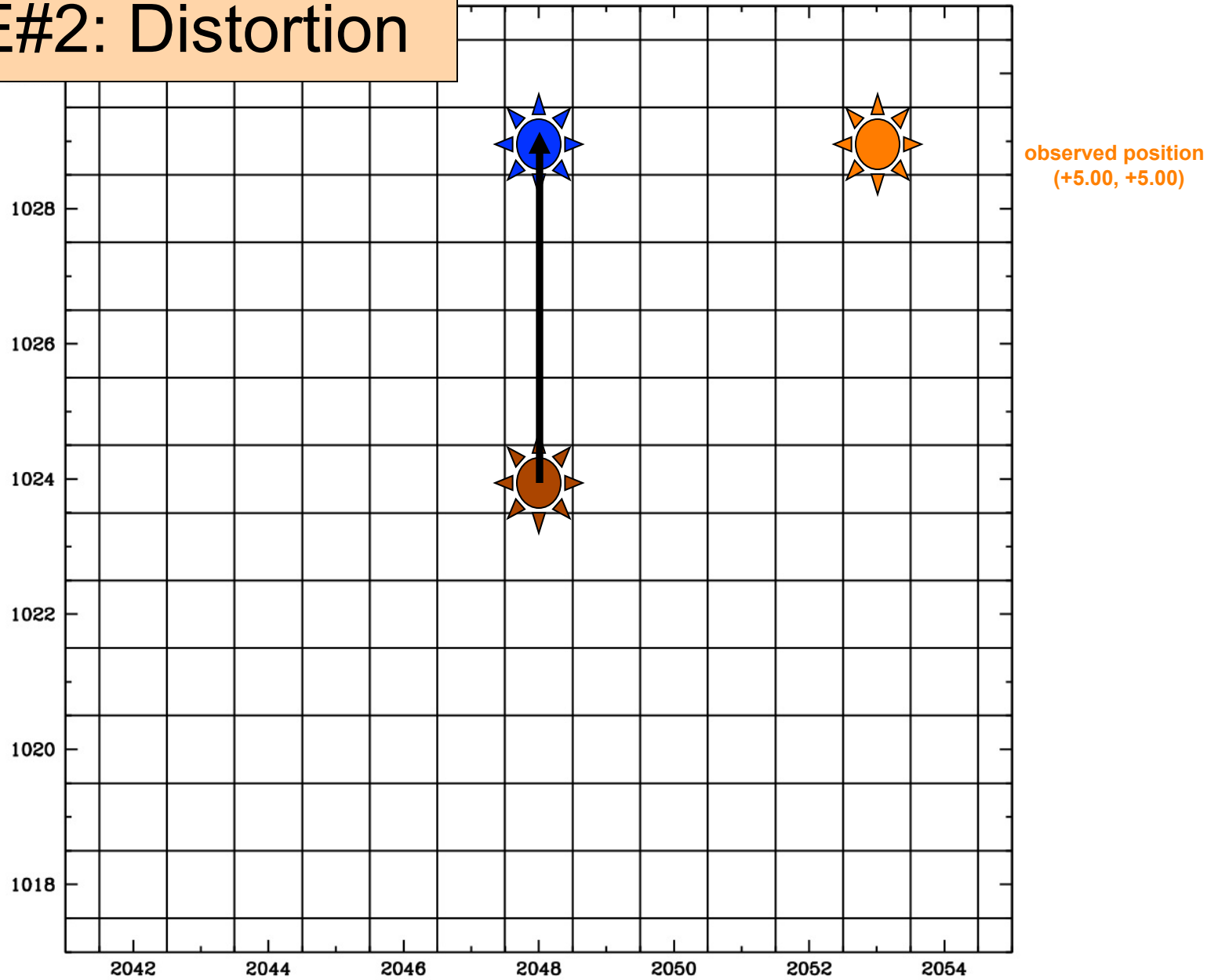
# Higher-Level PSF Issues... Pre-SM4

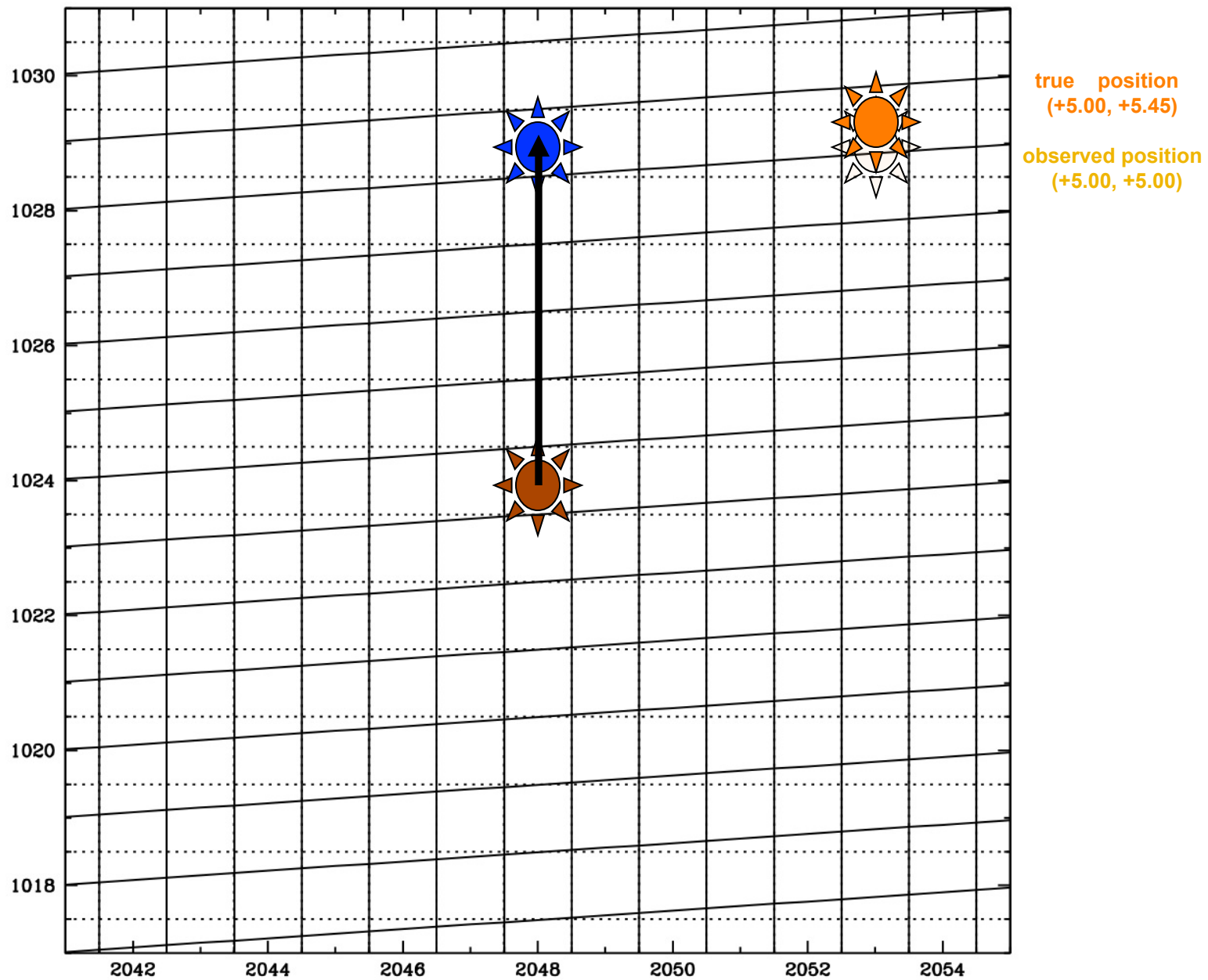
- **Spatial variability**
- **Time variability**
  - Breathing: +/- 2%
  - Hybrid models:
    - $\text{PSF}(x,y;t)=\text{PSF}(x,y)+\text{PSF}(t)$
    - Good for ACS, ok for UVIS
  - Long-term variability (ACS)
- **How to define “center” ?**
  - Peak? Centroid? Point of Symmetry?
  - Cross-talk with distortion
- **Pixel-response function:  $\Pi(\Delta x, \Delta y)$** 
  - Included naturally
- **Color variability: ~0.002 pixel (extreme: 0.02 pixel)**



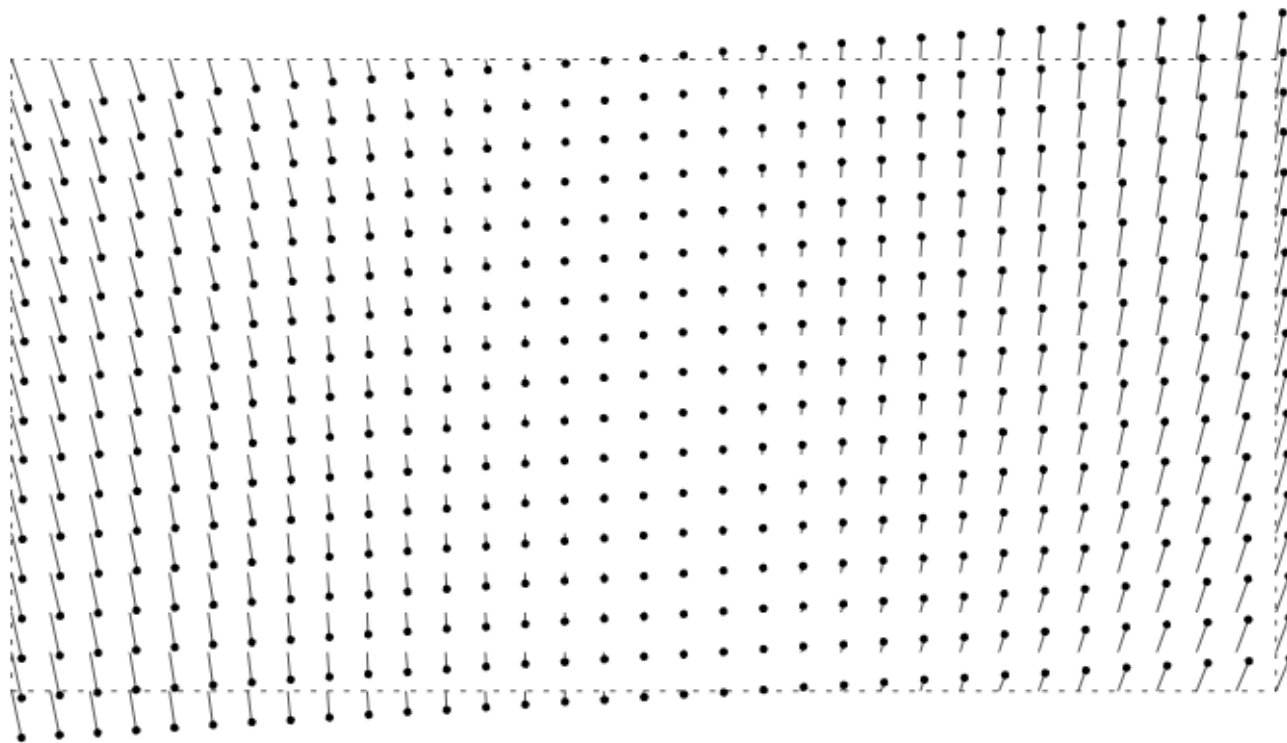
Post-SM4

# ISSUE#2: Distortion





**Distortion**

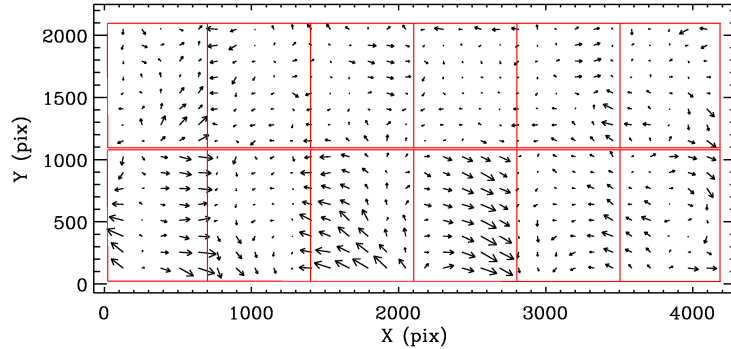


# WFC/ACS DISTORTION

# Sources of Distortion

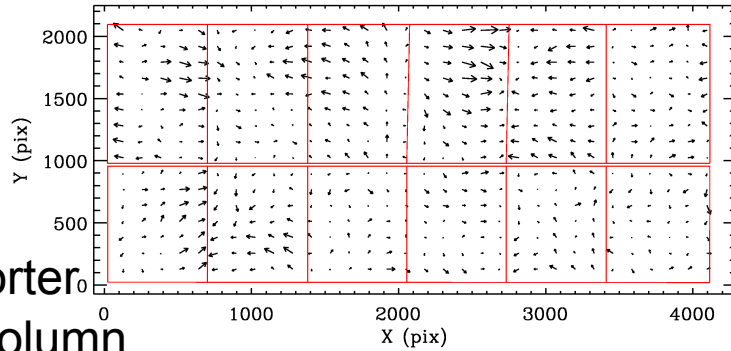
## 1) Geometric optics:

- Linear “skew”: 500 pixels over 2000  
→ Parallelogram pixels
- Non-linear: 50 pixels over 2000



## 2) Filters introduce distortion

- Offsets, scale changes
- “Fingerprint” of  $\sim 0.05$  pixel



## 3) Detector “stitching” defects

- WFPC2: every 34.1333<sup>th</sup> row 3% shorter
- ACS/WFC: pattern every 68.2666<sup>th</sup> column
- WFC3/UVIS: 2-D zones

**UVIS**

## 4) CTE losses...

- ACS Solution now available (UVIS coming soon)

**Need empirical approach...**  
Plot everything against  
everything else...

ISSUE#1: Undersampling/PSFs

ISSUE#2: Distortion

ISSUE#3...

# Transformations

## All HST astrometry is differential astrometry

- Guide-star precision  $\sim 0.5''$  (improved from  $1.5''$ !)
- No reference stars in typical field
- We never know the true pointing

## Always need to define a *local* reference frame

- Pixels/positions have only relative meaning.
- Choosing a frame/population you know something about
  - absolute  $\mu = 0$  (galaxies)
  - average  $\mu = \text{same}$  (clusters)
  - average  $\mu = \text{unchanging}$  (field)
- Allow for breathing effects
  - 6-param transformations, or go local

**ISSUE#1: Undersampling/PSFs**

**ISSUE#2: Distortion**

**ISSUE#3: Transformations**

## **Good News: All manageable issues**

### **Undersampling/PSFs:**

- Ways to model accurately, get 0.01-pixel positions
- Libraries available, usually sufficient

### **Distortion:**

- Stable, model available, small variations,  $\sim 0.01$  pixel

### **Transformations:**

- Can optimize for program

0.01 pixel error  
per exposure,  
can be made  
random

## **Bad news:**

**No one-size-fits-all solutions...**

# Astrometric Science with HST...

- 1) Cluster Membership**
- 2) Absolute motions
- 3) Internal motions in clusters
- 4) Microlensing applications**

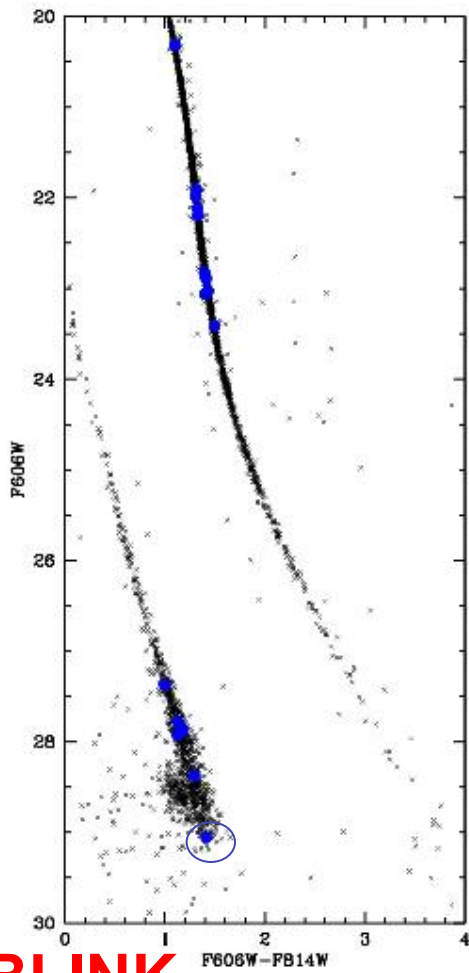
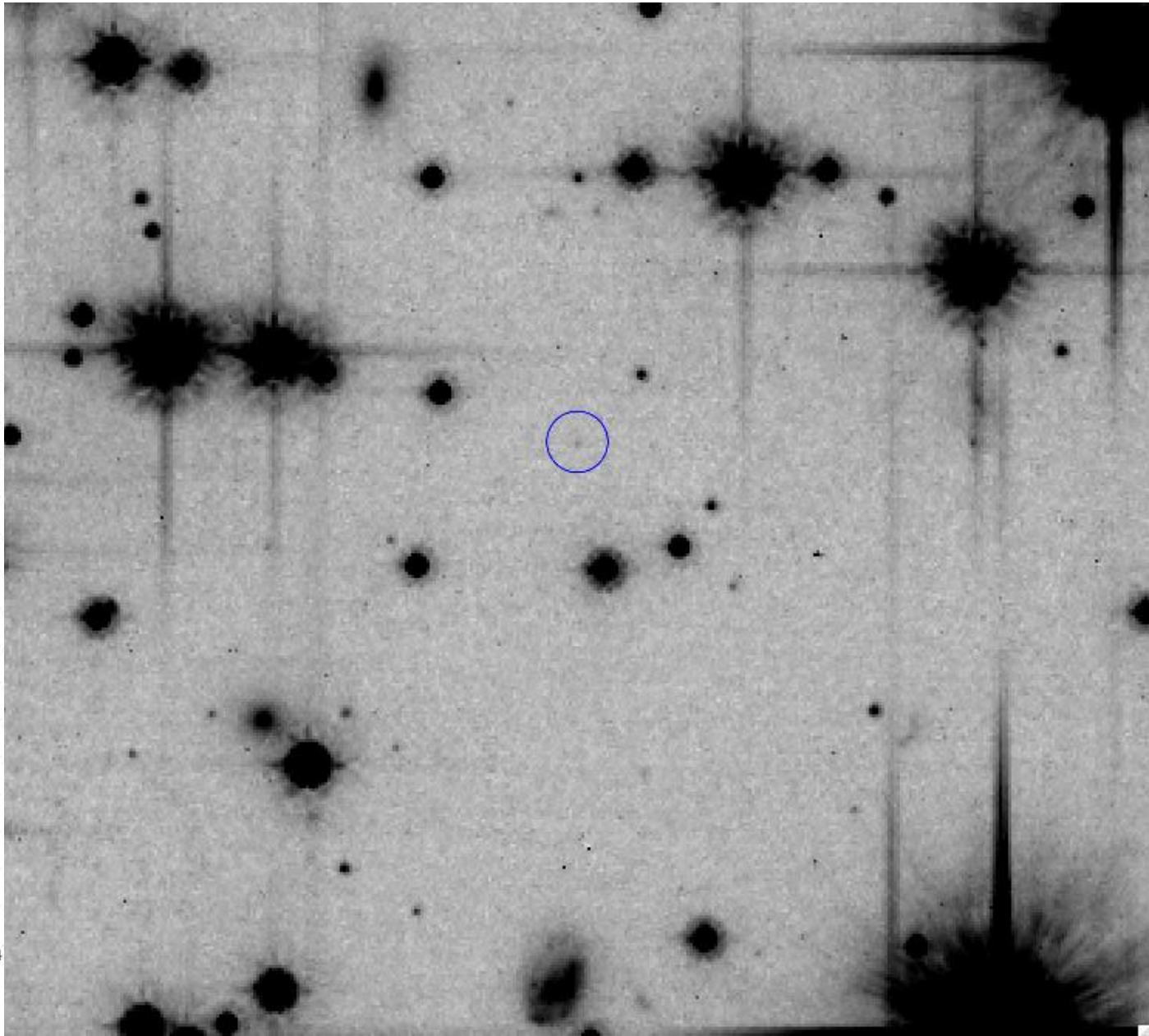


# 1) Bulk motions:

NGC6397

PI-Rich, UCLA

Proper-Motion  
Cleaning

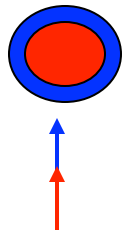


**BLINK**

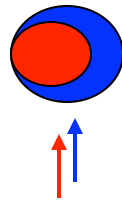
# 4) Microlensing Applications (breaking degeneracies)

## 1) Color-dependent centroid shift (1<sup>st</sup> moment)

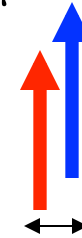
- Color difference between lens/source  $\rightarrow \mu$



During event



After event



$$f \times \mu = 0.6 \text{ mas/2yr}$$

Bennett et al 2006

OGLE-2003/BLG-235

MOA-2003/BLG-53

## 2) De-blending (measure 2<sup>nd</sup> moment)

## 3) Astrometry during the event

## **2) De-blending:**

**OGLE-2005-BLG-169**

**Epoch 1 HST Observations**

# WFC3/UVIS Image



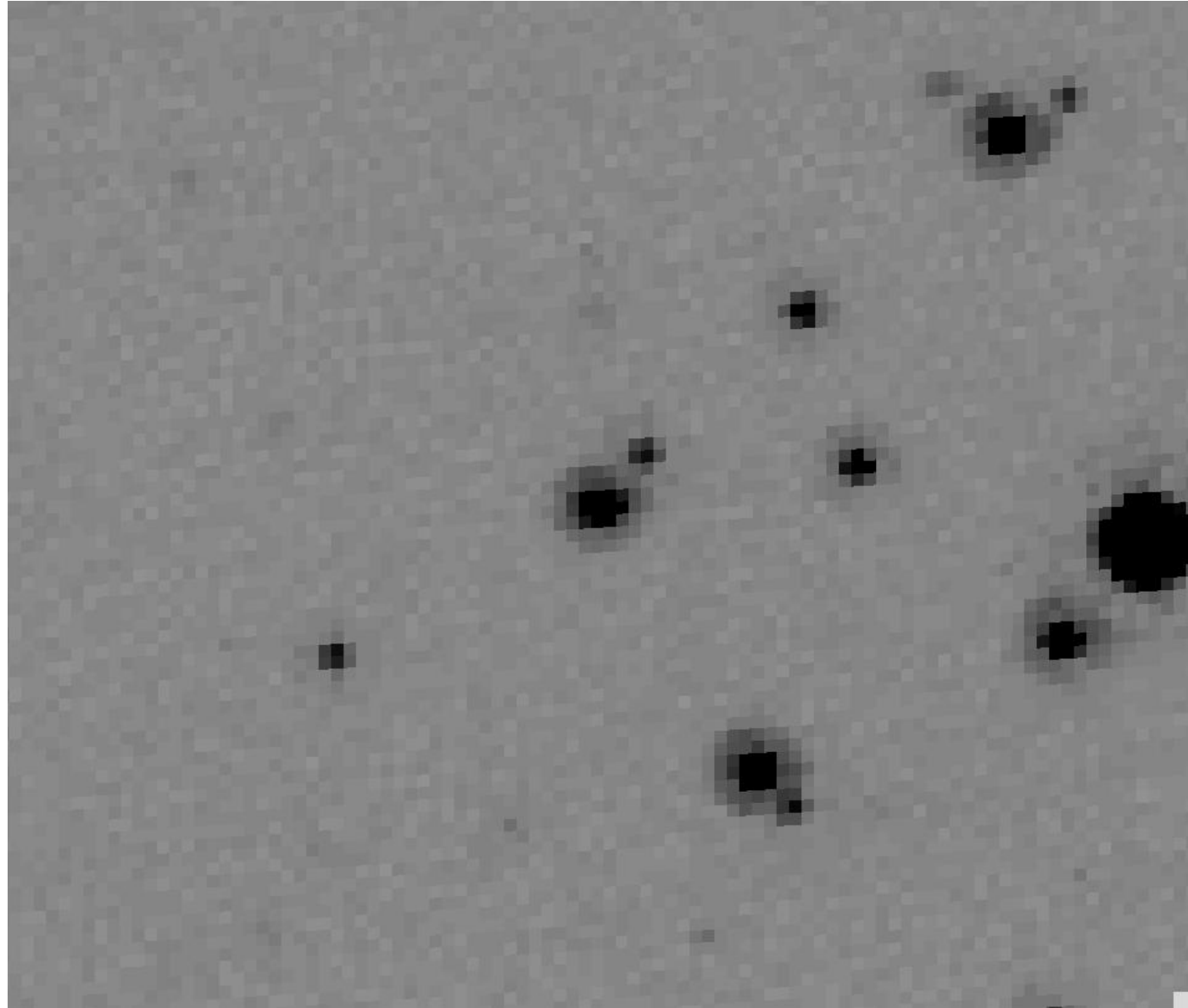
**OGLE-2005-BLG-169L**  
-Wiki: 2000 kpc “bulge” star  
-Uranus-mass extrasolar  
planet

## HST IMAGES

-GO-12541 (PI-Bennett)  
-2 orbits Oct 2011  
- 6xB, 8xV, 7xI  
- decently dithered

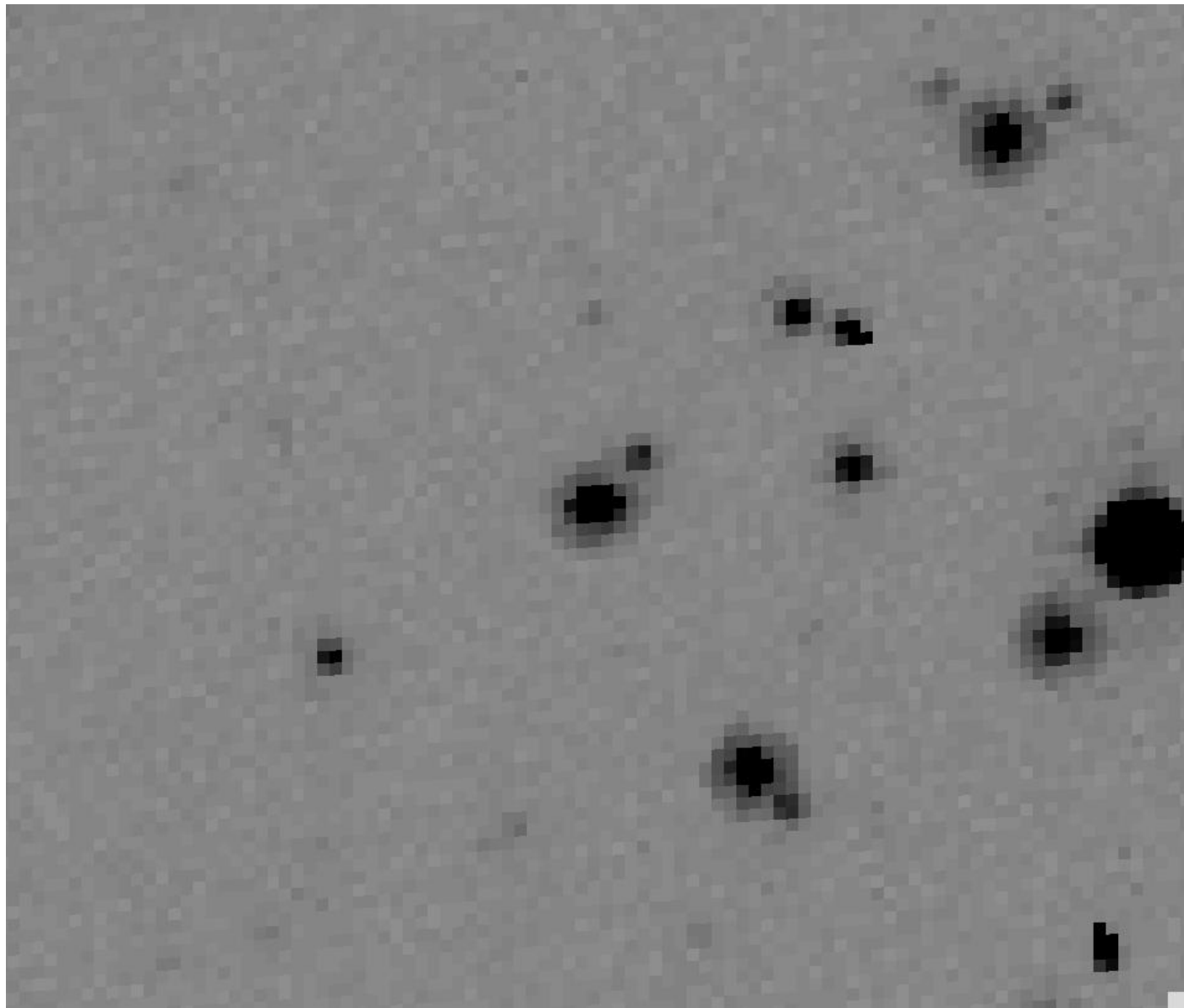
# Seven F814W Observations

$i_1$



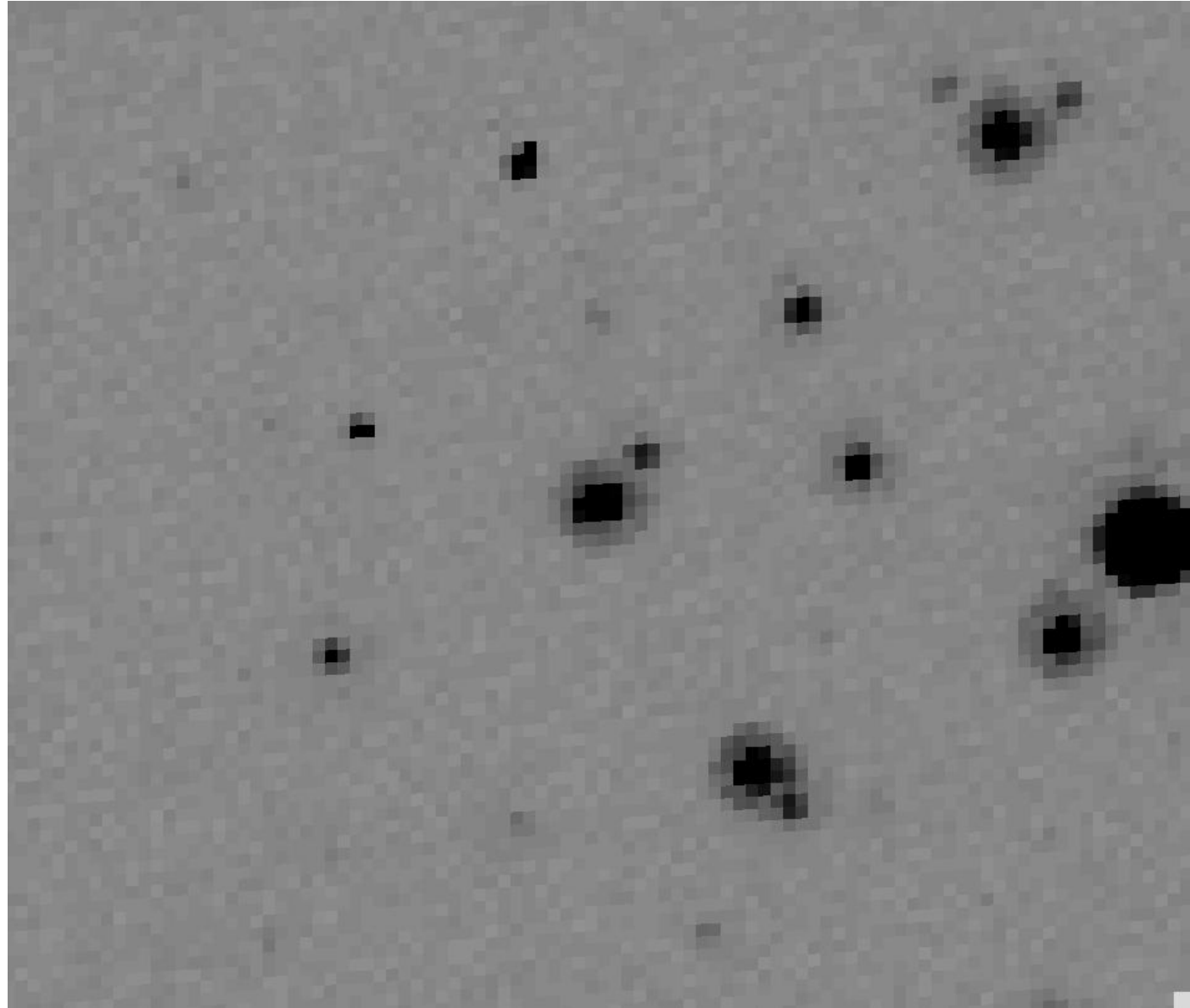
# Seven F814W Observations

$i_2$



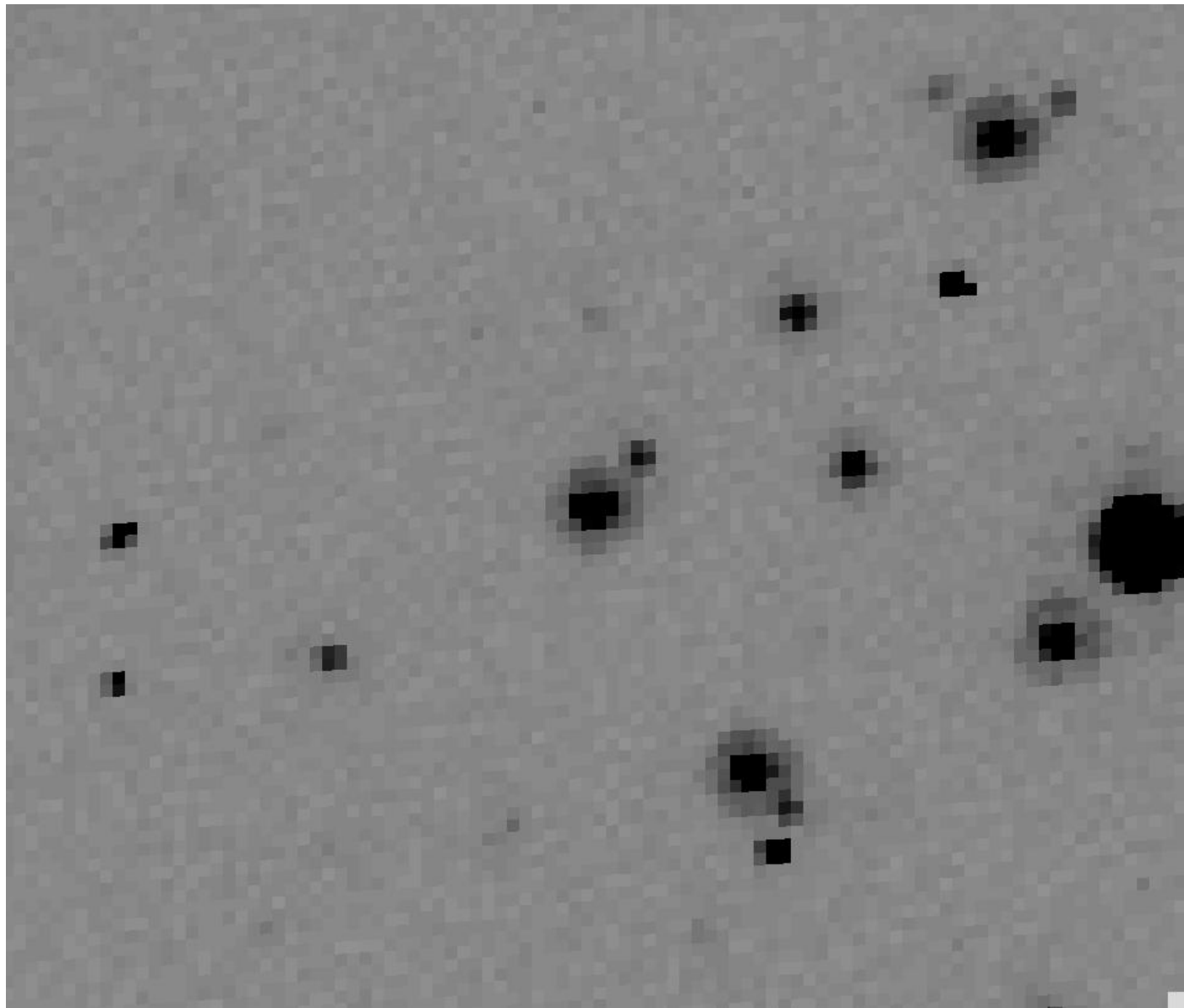
# Seven F814W Observations

$i_3$



# Seven F814W Observations

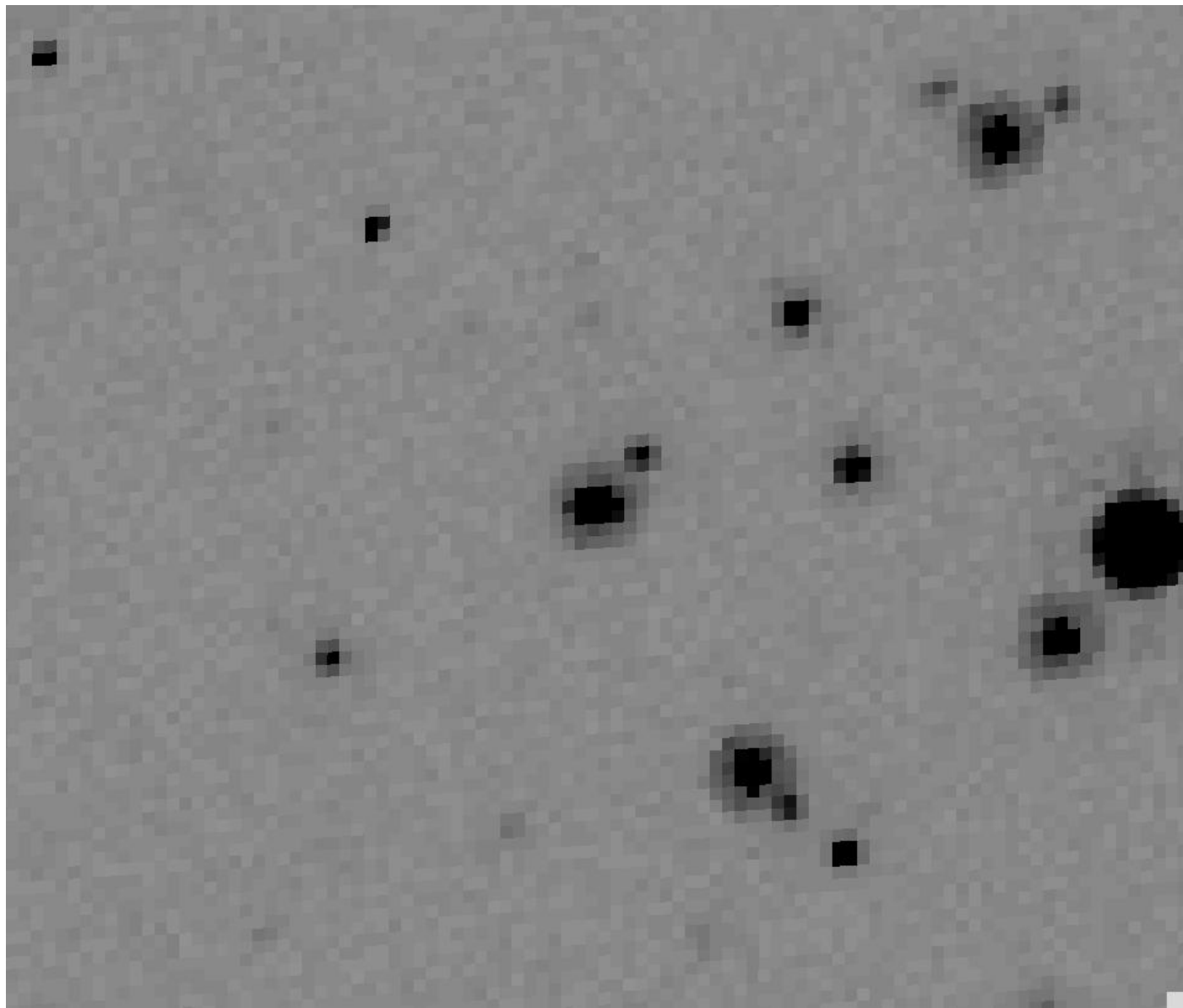
$i_4$





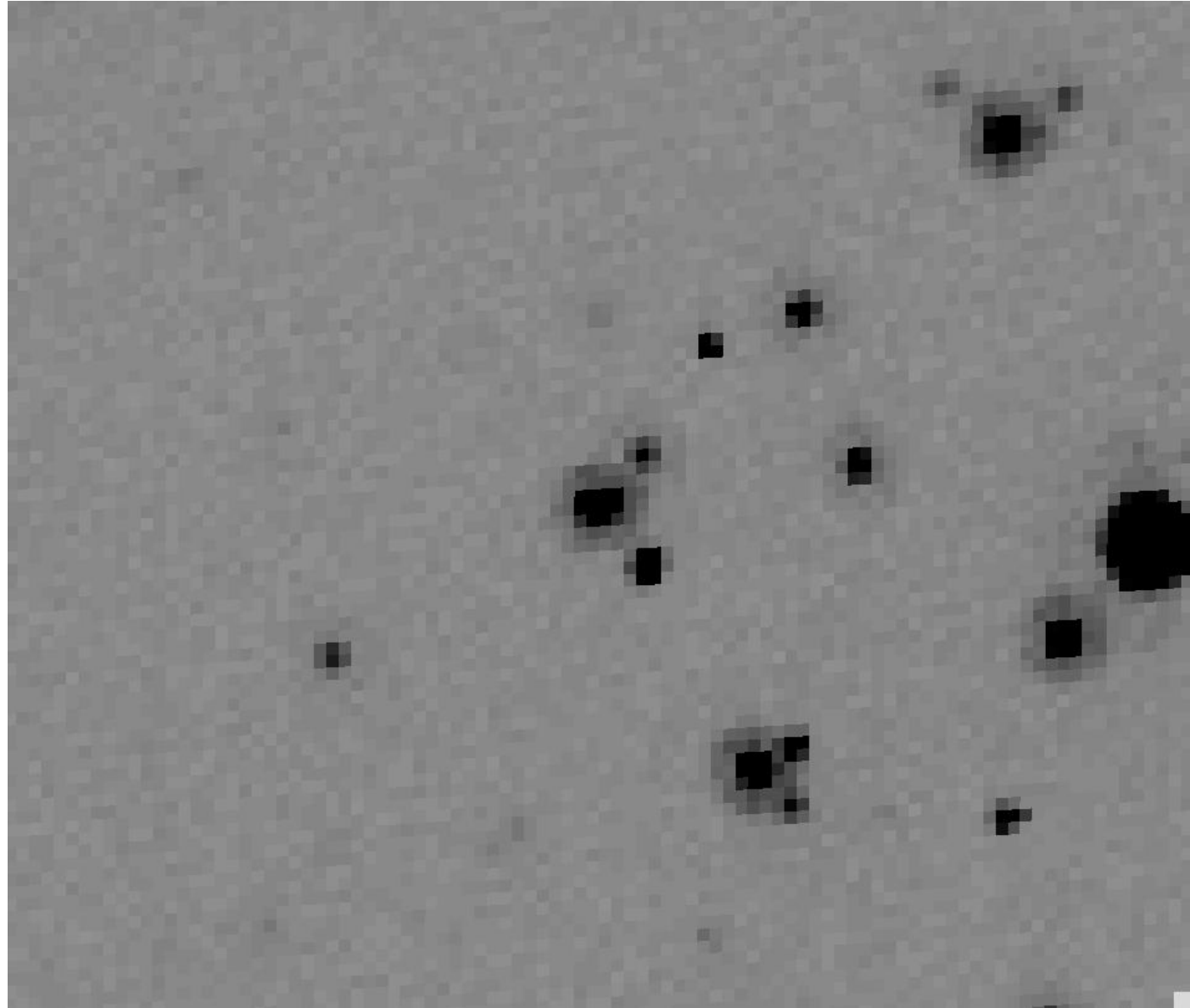
# Seven F814W Observations

$i_5$



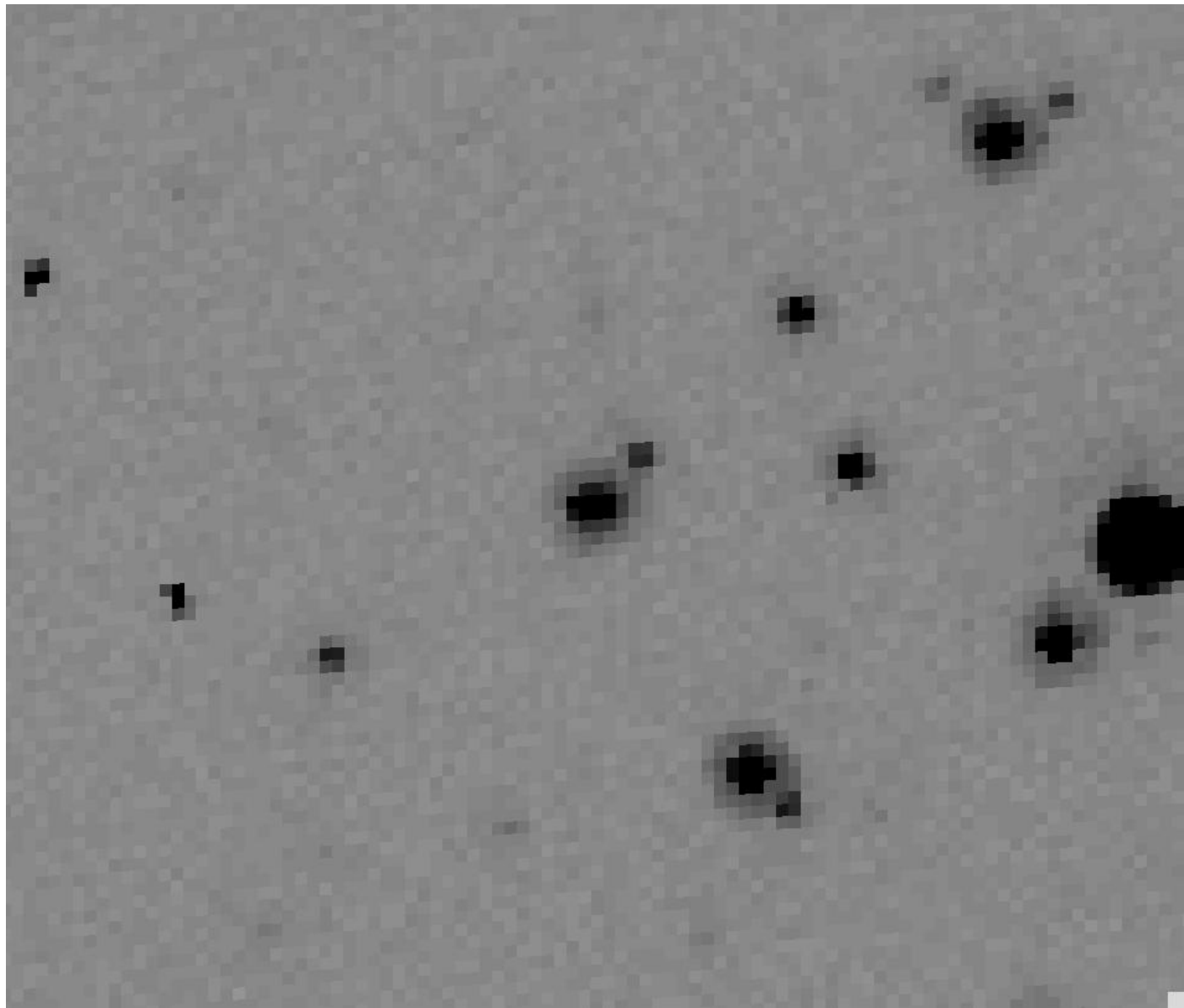
# Seven F814W Observations

$i_6$

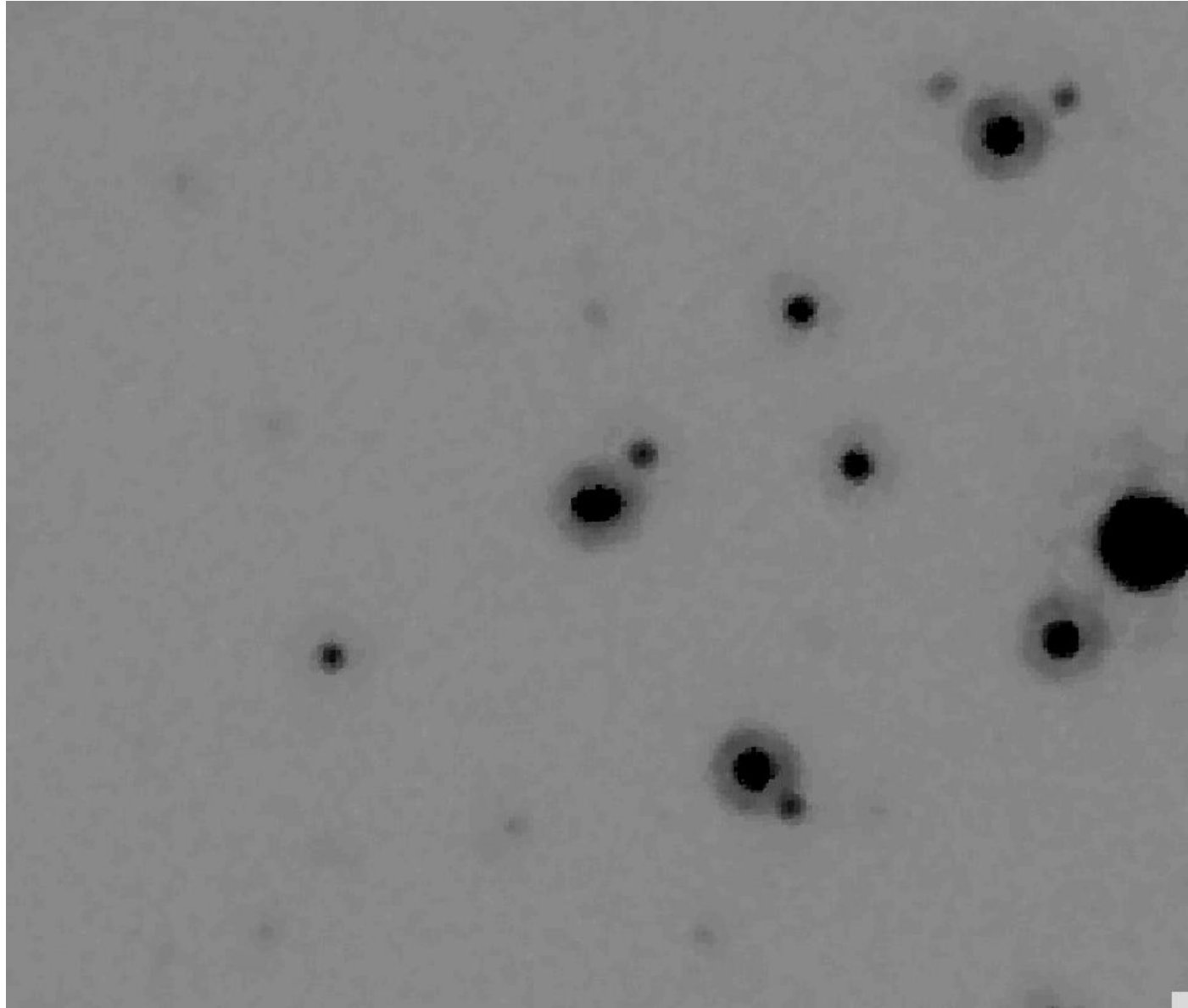


# Seven F814W Observations

$i_7$

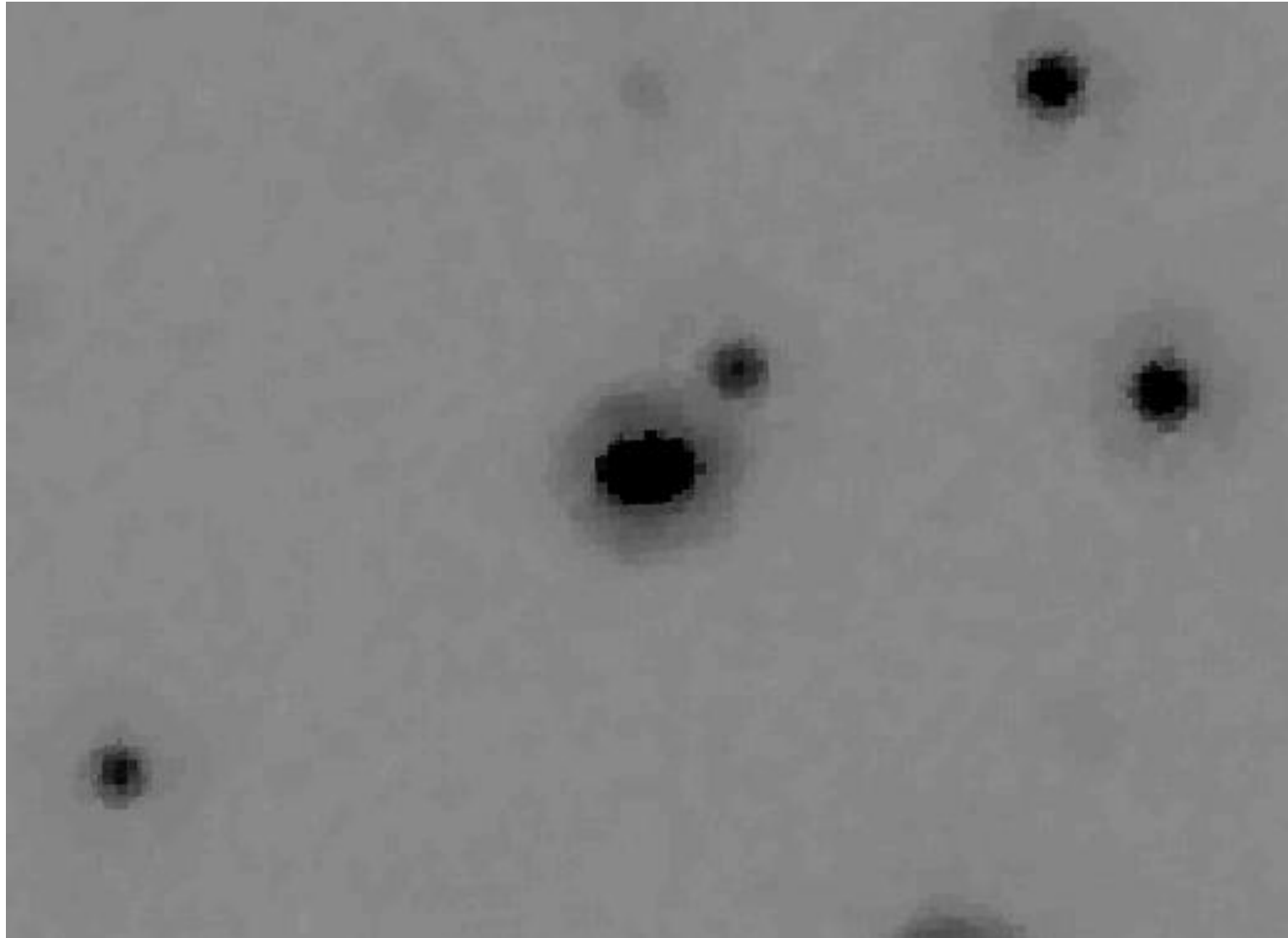


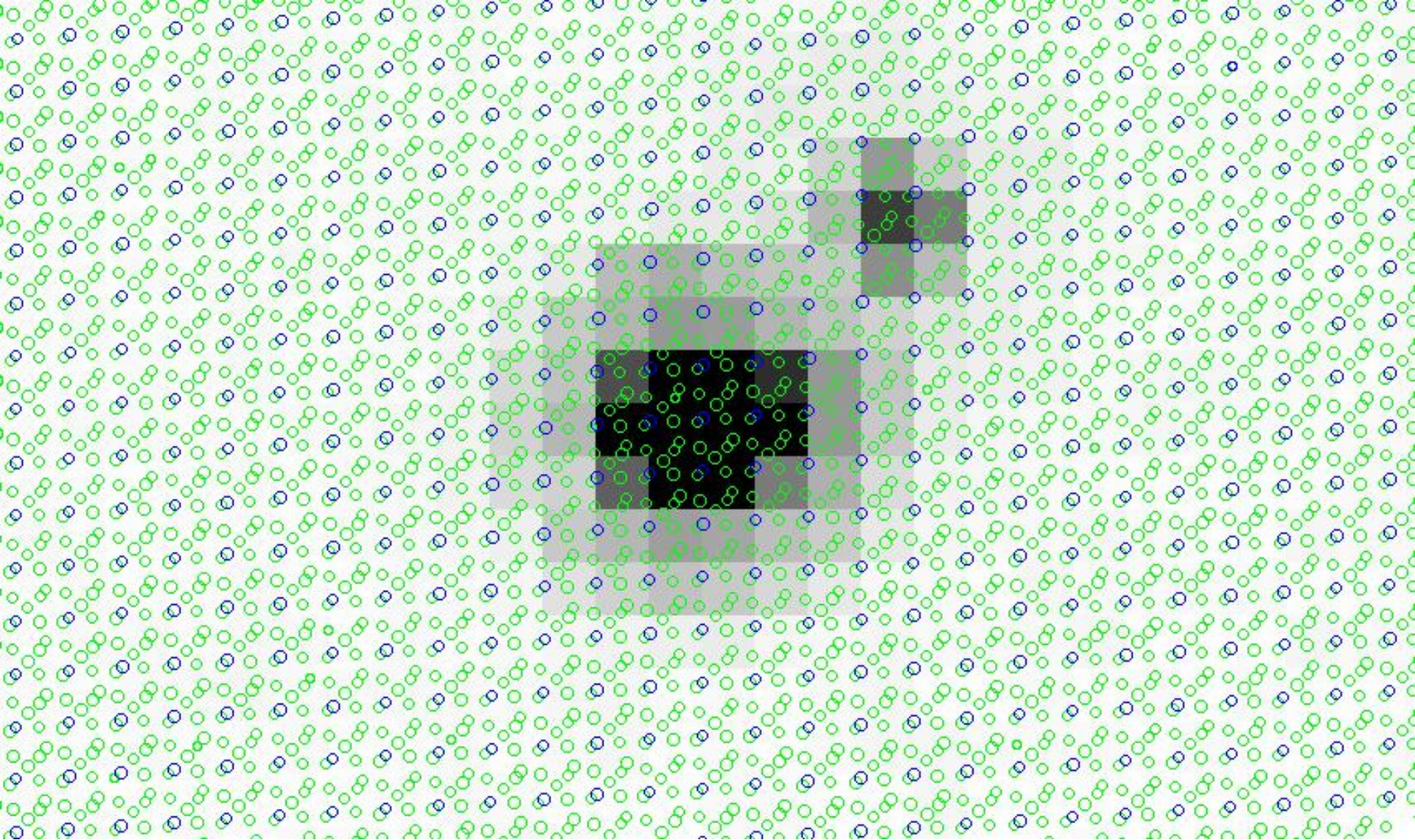
# Stacked F814W Observations



# Zoomed F814W Stack

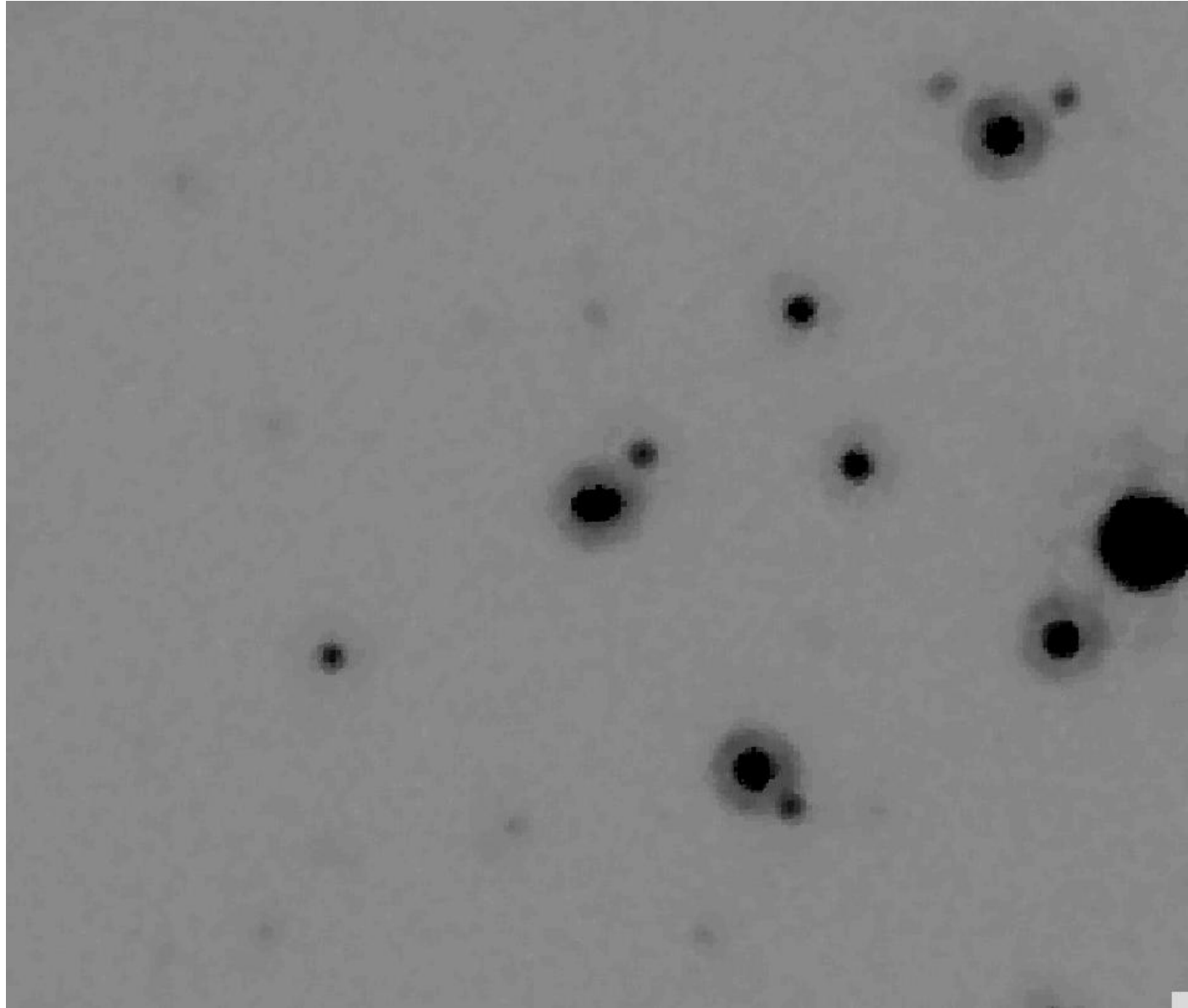
Source  
*looks*  
elongated  
relative to  
neighbors





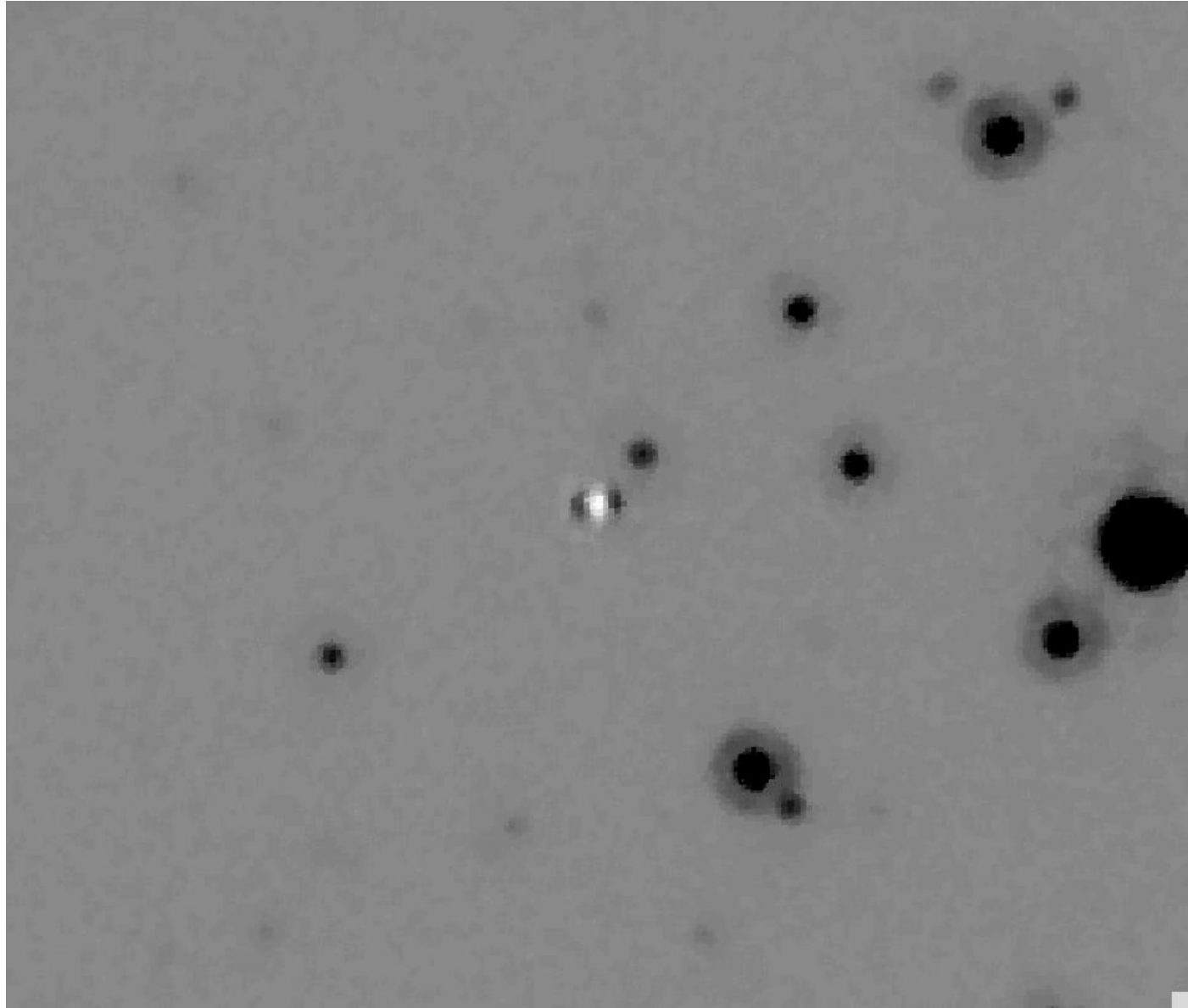
**Achieved sub-pixel sampling**

# Stacked F814W Observations



# Subtracted F814W Stack

Residuals  
in  $X$  when  
we subtract  
a PSF from  
each image  
and stack...

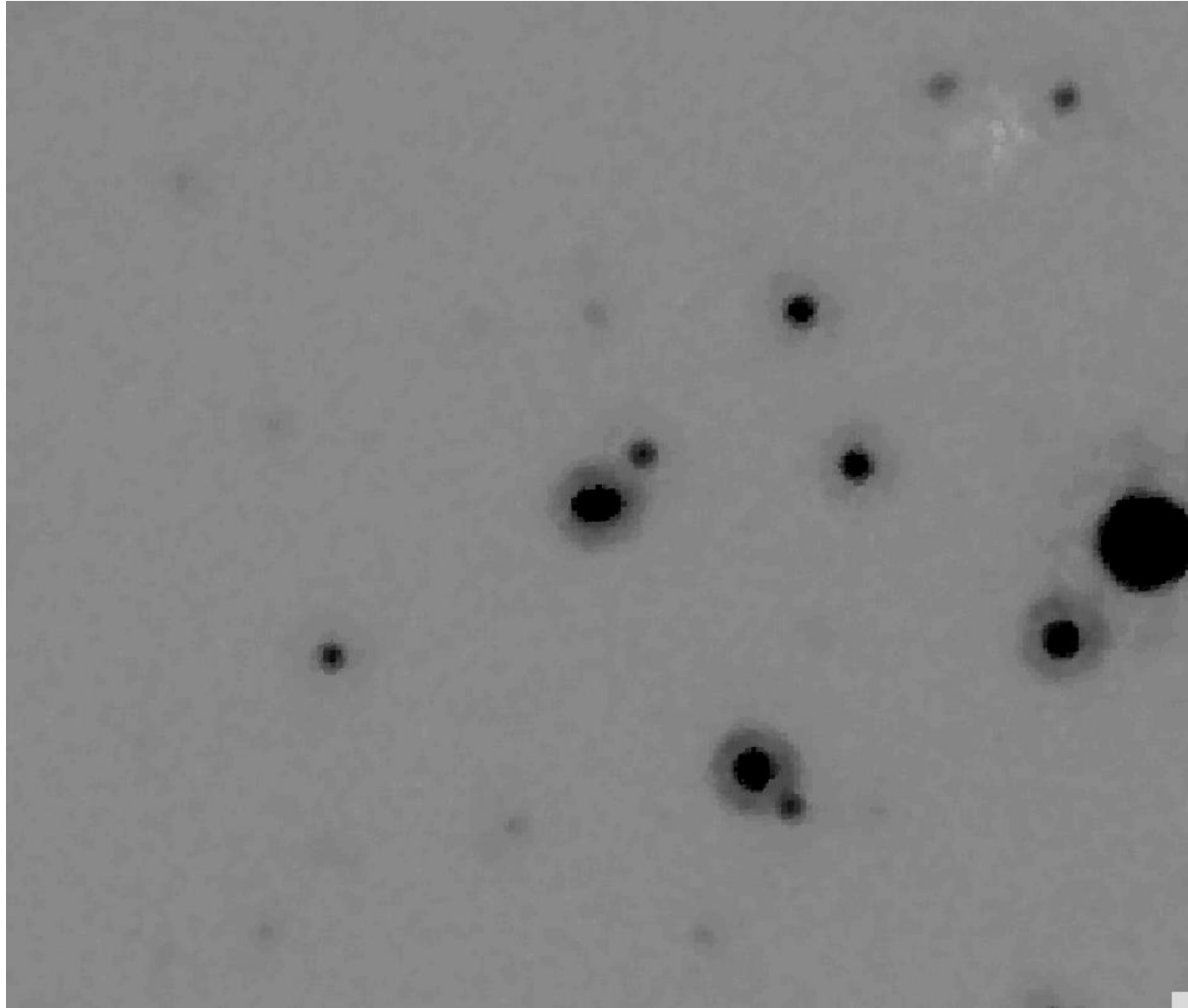




# Subtracted Neighbor...

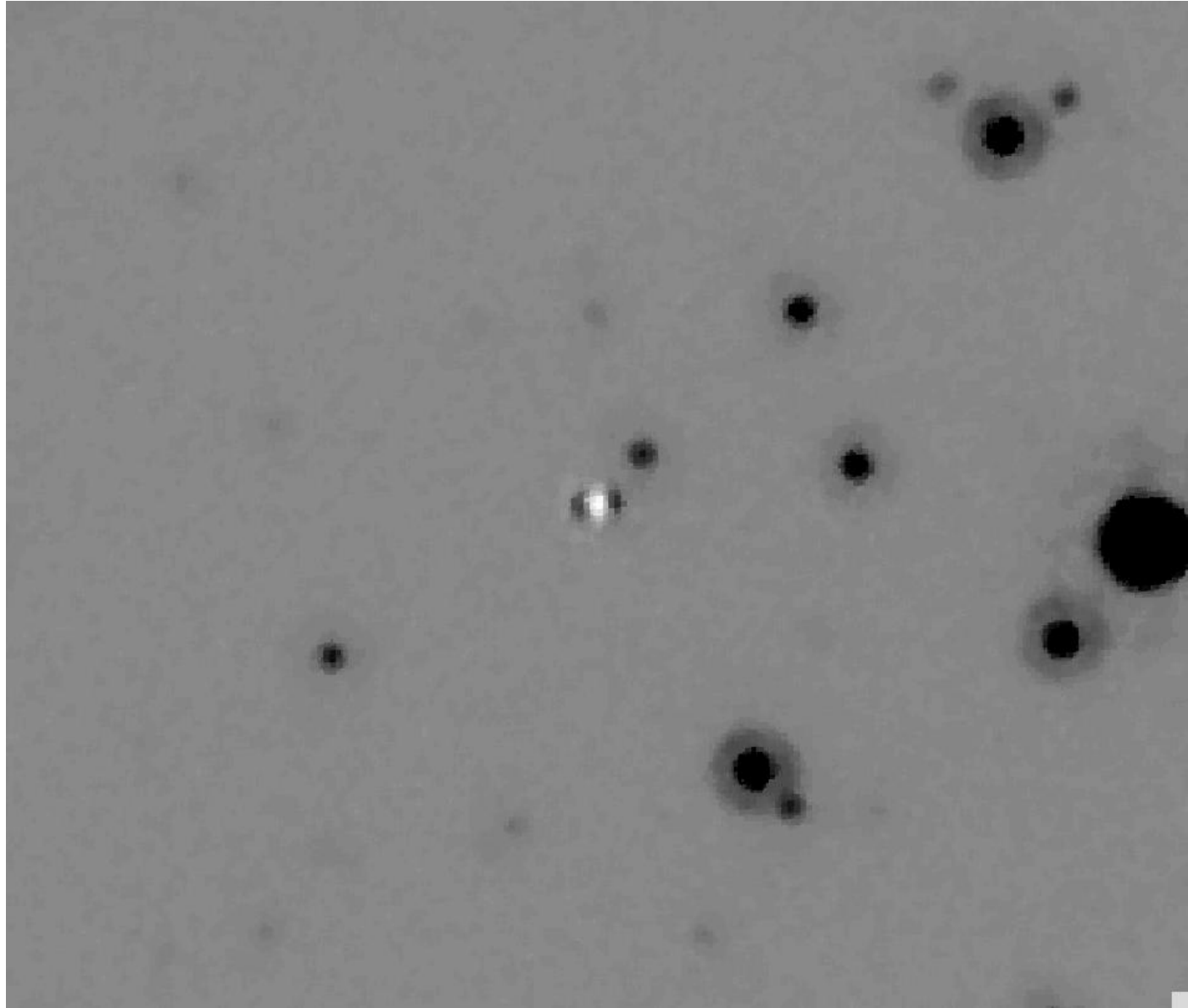
**PSF IS  
GOOD!**

Almost *no*  
residuals  
When we  
Subtract a  
PSF from a  
(brighter)  
neighbor



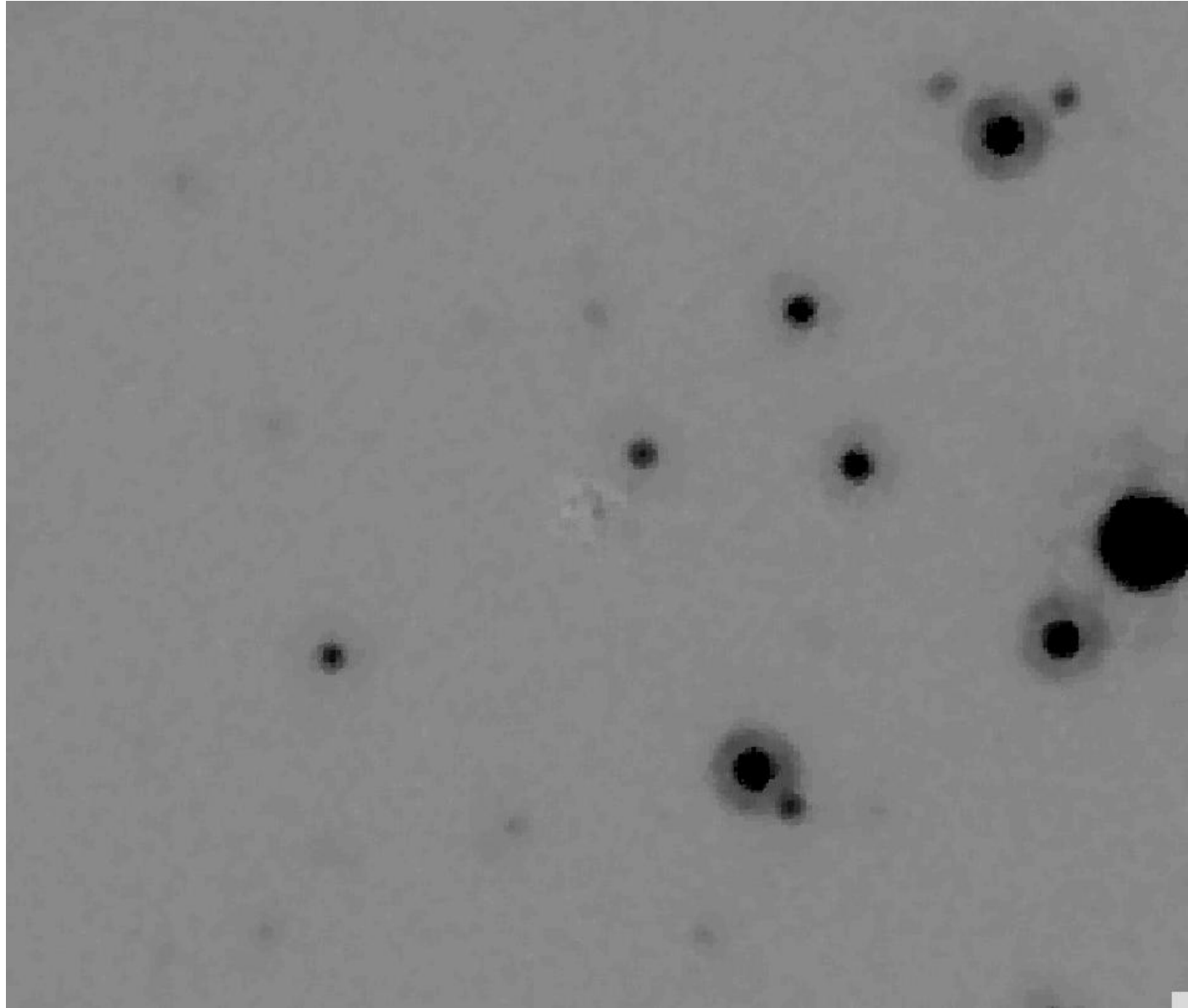
# Subtracted F814W Stack

This means  
that the  
residuals of  
the target-star  
subtraction  
are *real*.



# 2-Source Subtracted F814W

We get very good subtraction residuals when we fit for *two* sources



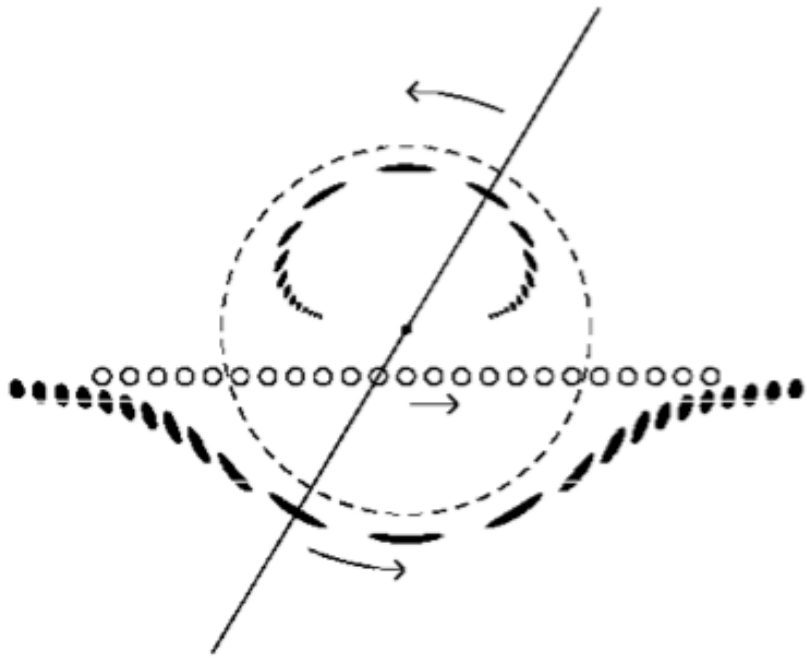
# Two-source solution:

- Offset consistent in the B, V and I data:
  - $\Delta x = 1.25$  pixels = 50 mas ( $\Delta T = 6$  yrs)
  - $\Delta y = 0.25$  pixel = 10 mas
  - FLUX:

	(left)	(right)
• F814W	3392 e <sup>-</sup>	3276 e <sup>-</sup>
• F555W	2158 e <sup>-</sup>	3985 e <sup>-</sup>
• F438W	338 e <sup>-</sup>	1029 e <sup>-</sup>

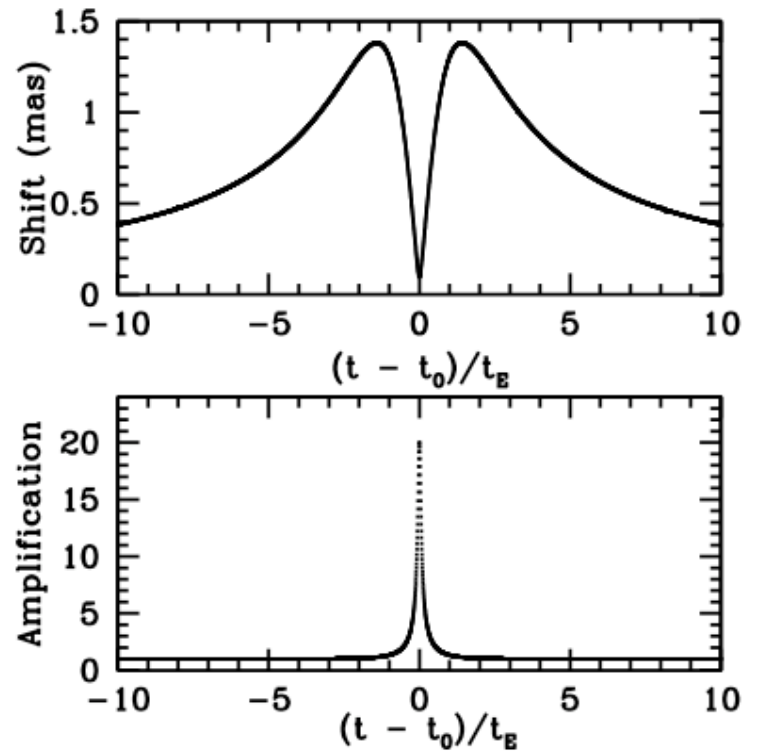
### 3) Astrometry during the event

- Long-duration events: BH? NS? WD? BD?
- Kailash Sahu (PI)
  - Some long-duration event follow ups with HST
    - OGLE-2007-BLG-224
    - MOA-2009-BLG-260
    - MOA-2010-BLG-235
    - MOA-2010-BLG-356
    - MOA-2010-BLG-482
  - GO-12586: Finding our own events
    - 192 orbits over 3 cycles



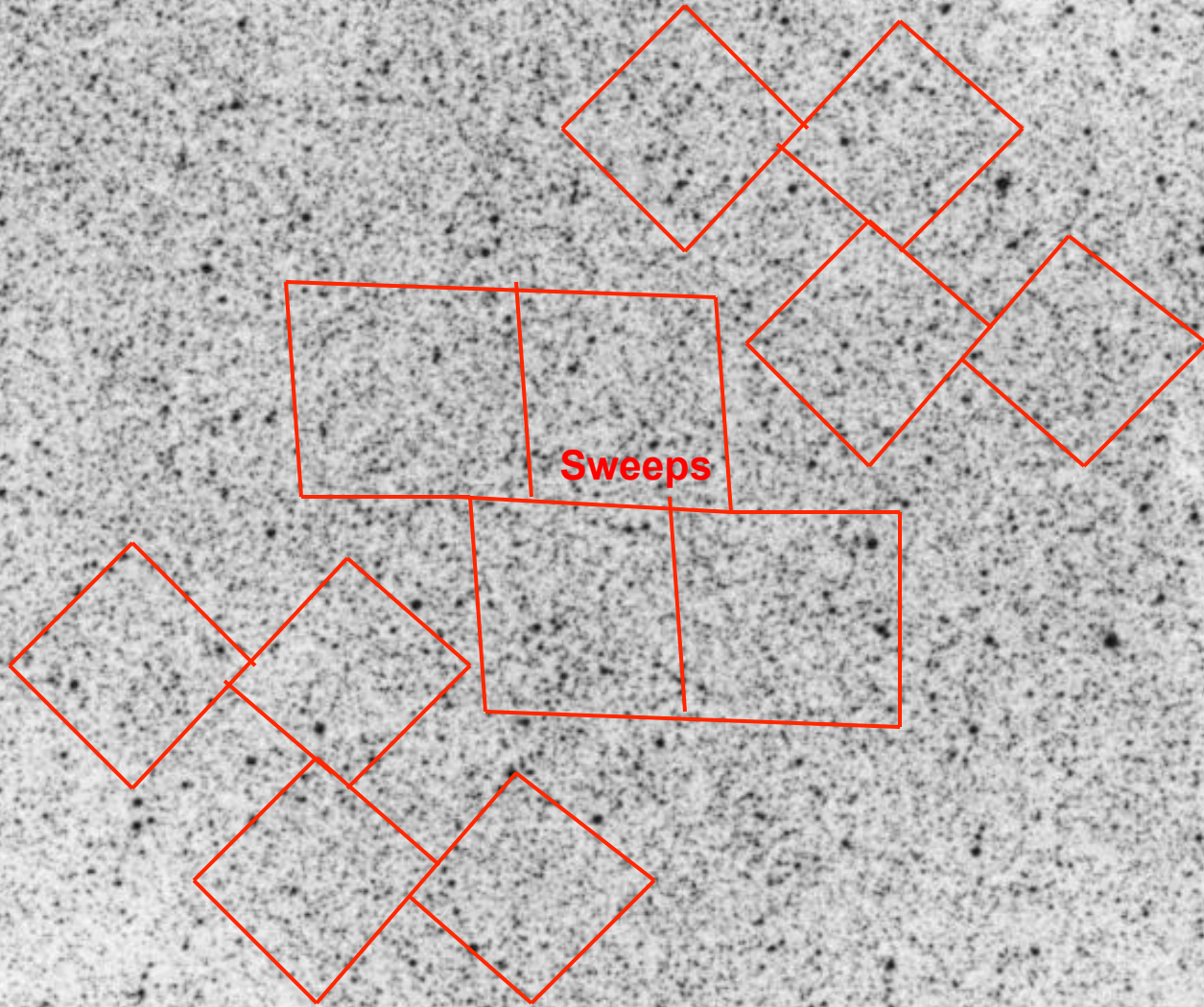
**Schematic of event**

Duration of event  $\propto \text{mass} \times \mu$   
 Astrometric offset  $\propto \text{mass}$

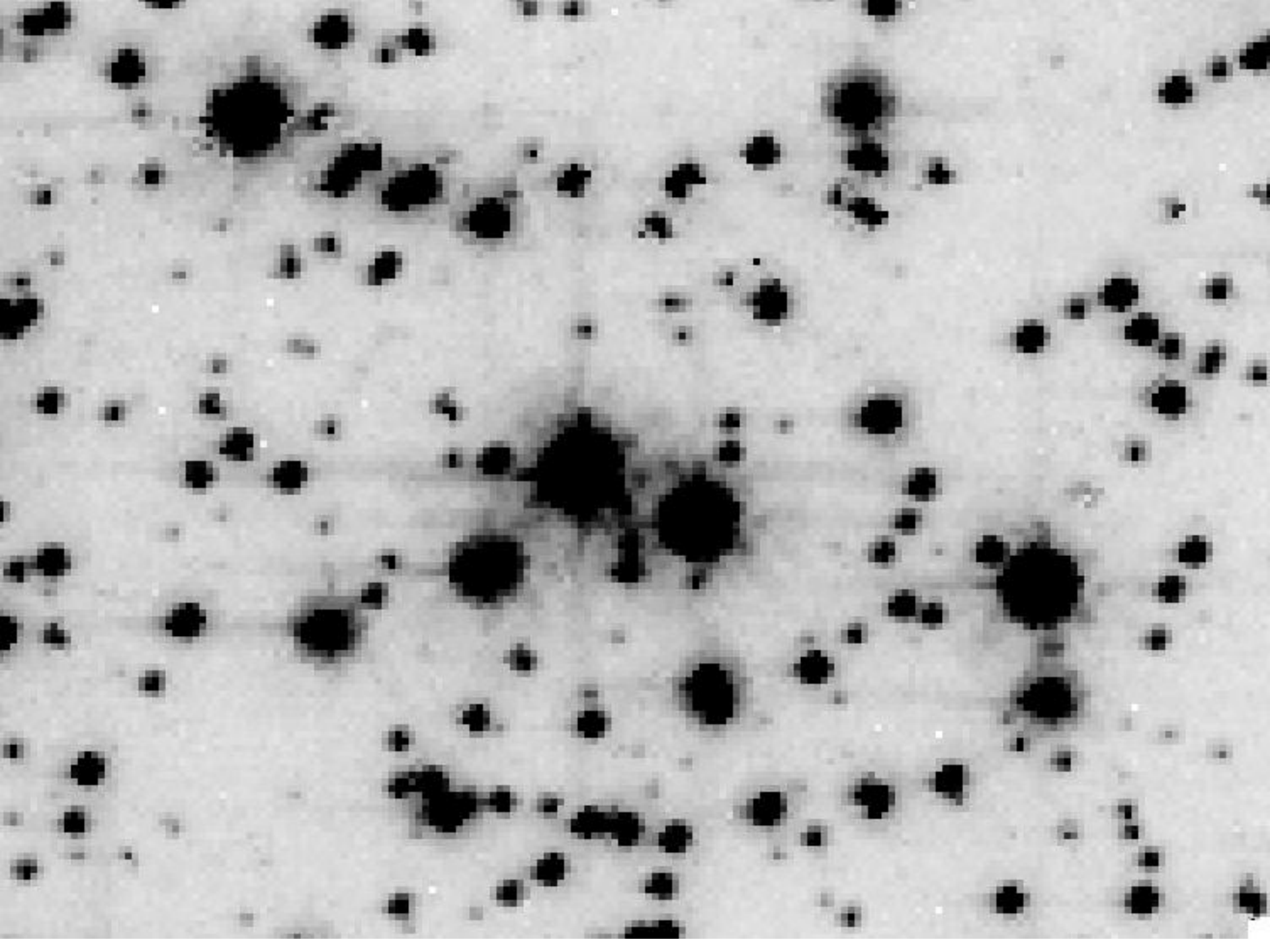


**Photometry/Astrometry**

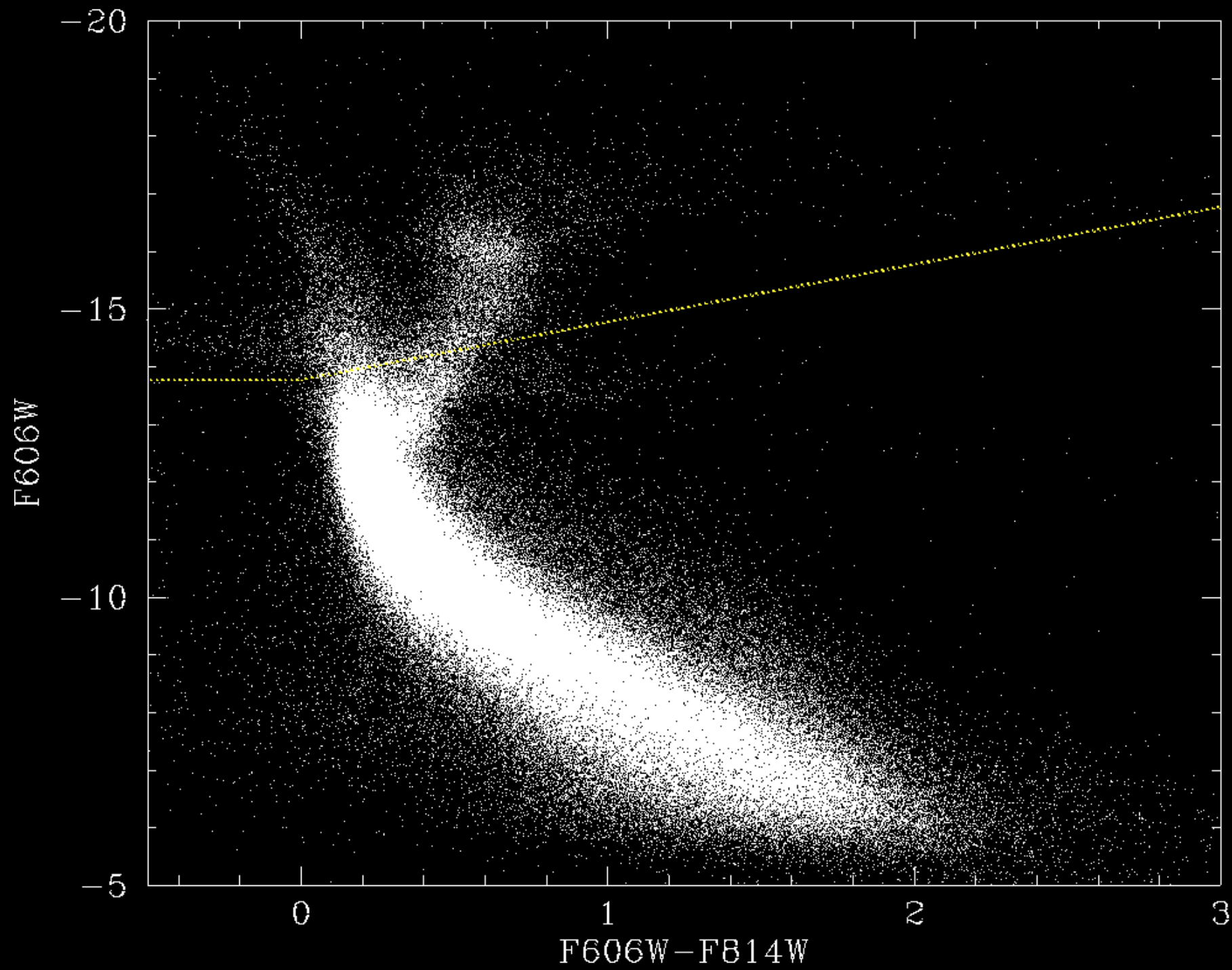
**Fast BH, NS, WD or slow BD?**



**Sweeps**







# OBSERVING STRATEGY

- **NUMBER OF TARGETS**

- Each ACS field has ~200,000 stars
  - 50% have S/N > 100
- Each WFC3/UVIS field has 150,000 stars
- **Total of > 1,500,000 stars**

- **OBSERVING CADENCE**

- Optimized for long-duration events
- One visit every 2 weeks over two 4-month windows
  - 64 visits per year

- **EXPECTATIONS:** (54 / 120 events “astrometric”)

- 18 events due to BHs
- 14 due to NSs
- 22 due to MS stars.... **STARTS IN APRIL!**

# APPLICATIONS TO WFIRST

- HST programs: hard to get time!
  - WFIRST will do for all sources
- Success with HST PSF encouraging
  - Model static part
  - Perturb with time-variable part
  - Need “semi-crowded” star field
    - Construct basis functions for PSF / GC
    - Long stare
    - WL will ❤️  $\mu\text{L}$ !
  - Demo software (Sahu program)



Omega Cen: a Ground-Based Image (Lehman)



GB → ACS → UVIS → PMs